

## S2 Final Examination (2024-2025)

Mathematics

(1 hour 30 minutes)

Date: 4<sup>th</sup> June 2025

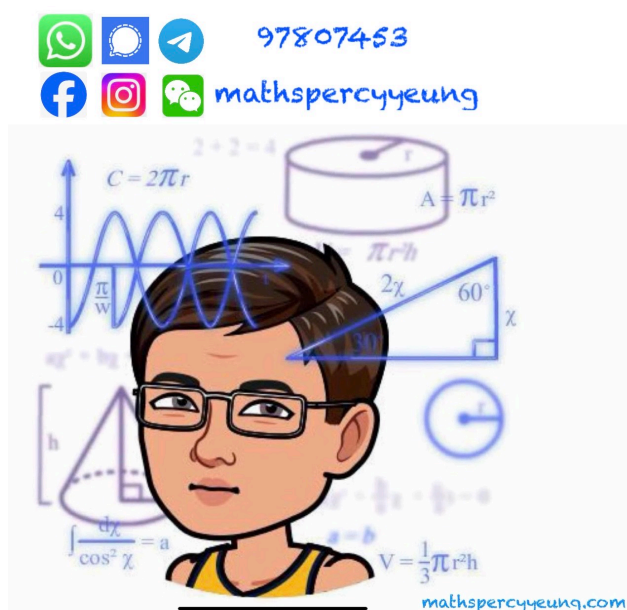
Time: 8:30 a.m. – 10:00 a.m.

Name: \_\_\_\_\_

Class: \_\_\_\_\_ No. : \_\_\_\_\_

### Instructions to students:

1. This paper consists of THREE parts, Conventional Questions, Multiple-choice Questions and Bonus Question. There are Section A and Section B in Conventional Questions. Section A carries 62 marks. Section B carries 18 marks. Multiple-choice Questions carry 20 marks. Bonus Question carries 3 marks.
2. The maximum score of this paper is 100.
3. Attempt ALL questions in Conventional Questions and Multiple-choice Questions. Write your answers in the spaces provided in this Question / Answer Book.
4. Unless otherwise specified, all workings must be clearly shown.
5. Unless otherwise specified, numerical answers should either be exact or correct to 3 significant figures.
6. The diagrams in this paper are not necessarily drawn to scale.



**Conventional Questions****Section A (62 marks)**

1. Factorize

(a)  $4x^2 - 4x + 1$ ,

(b)  $4x^2 - 4x + 1 - 9y^2$ .

(3 marks)

2. Simplify the following expressions.

(a)  $\frac{5h+10}{7k^2} \times \frac{14k}{2+h}$

(b)  $\frac{2x}{3} + \frac{3}{2x}$

(4 marks)

3. Consider the formula  $a + 3 = \frac{1-a}{b}$ .

- Make  $a$  the subject of the formula.
- If  $b = 3$ , find  $a$ .

(4 marks)

4. Simplify each of the following and rationalize the denominator of the result if necessary.

(a)  $\sqrt{18}$

(b)  $(2 - \sqrt{2})^2$

(c)  $\sqrt{3}(\sqrt{27} + \sqrt{8})$

(d)  $\frac{24}{\sqrt{32}}$

(7 marks)

5. In Figure 1,  $AFB$  is a straight line. If  $EA = EF$ , find  $x$  and  $y$ .

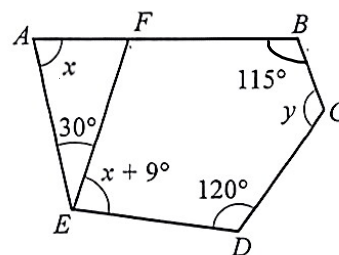


Figure 1

(5 marks)

6. In Figure 2, the area of sector  $OAB$  is  $12\pi \text{ cm}^2$ .
- Find the radius of the sector  $OAB$ .
  - Find the perimeter of the sector  $OAB$  in terms of  $\pi$ .

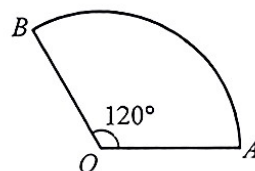


Figure 2

(4 marks)

- (3 marks)

- (5 marks)



9. Figure 3 shows a map of a route from  $A$  to  $B$ . The length of the route on the map is 53 cm.

- (a) Find the actual length of the route in m.
- (b) Mr Lau runs from  $A$  along the route at an average speed of 150 m/min. Can he arrive at  $B$  within two hours? Explain your answer.

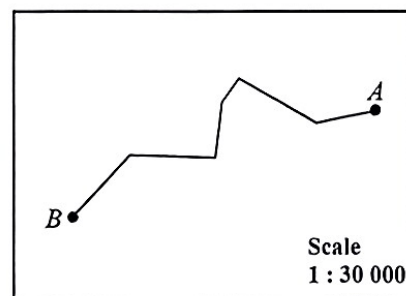


Figure 3

(4 marks)

10. Prove that  $\tan 45^\circ + \tan^2 \theta \equiv \frac{1}{\sin^2 (90^\circ - \theta)}$ .

(4 marks)

11. In Figure 4,  $BNC$  is a straight line.

- (a) Find  $BN$ . (Leave the answer in surd form.)  
 (b) Find  $\theta$ .

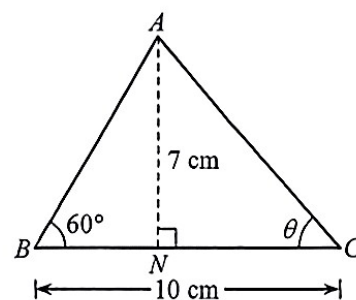


Figure 4

(4 marks)

12. Figure 5 shows the graph of the equation  $2x + 3y - 15 = 0$ . The graph cuts the  $x$ -axis at  $A$ .

- (a) Find the coordinates of  $A$  and  $B$ .  
 (b) Alice draws the graph of the equation  $x + 3y - 18 = 0$  on the same figure. Does the graph pass through  $B$ ? Explain your answer.

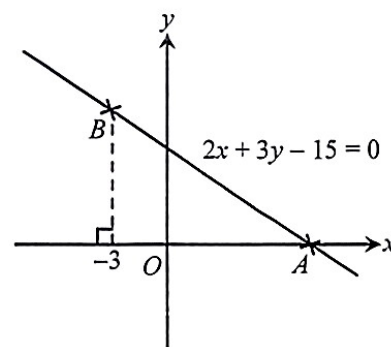


Figure 5

(4 marks)

(a) Prove that  $\triangle ABC \sim \triangle DCA$ .

(b) Find  $AD$  and  $CD$ .

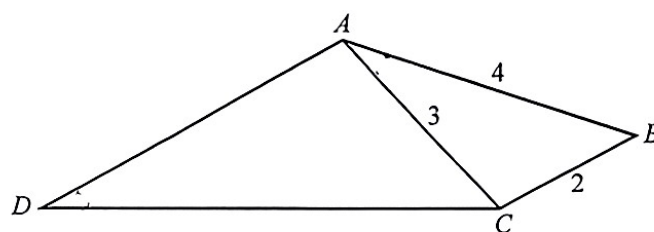


Figure 6

(5 marks)

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14. The frequency distribution table and the cumulative frequency distribution table below show the distribution of the time taken to finish an assignment by a group of students.

<i>Time taken (minutes)</i>	<i>Frequency</i>
36 – 45	$a$
46 – 55	$2a$
56 – 65	$b$
66 – 75	$q$

<i>Time taken less than (minutes)</i>	<i>Cumulative frequency</i>
45.5	2
55.5	$p$
65.5	$q$
75.5	$2q$

It is given that the percentage of the students takes less than 55.5 minutes to finish the assignment is 18.75%.

(a) Find  $p$ ,  $q$  and  $b$ .

(3 marks)

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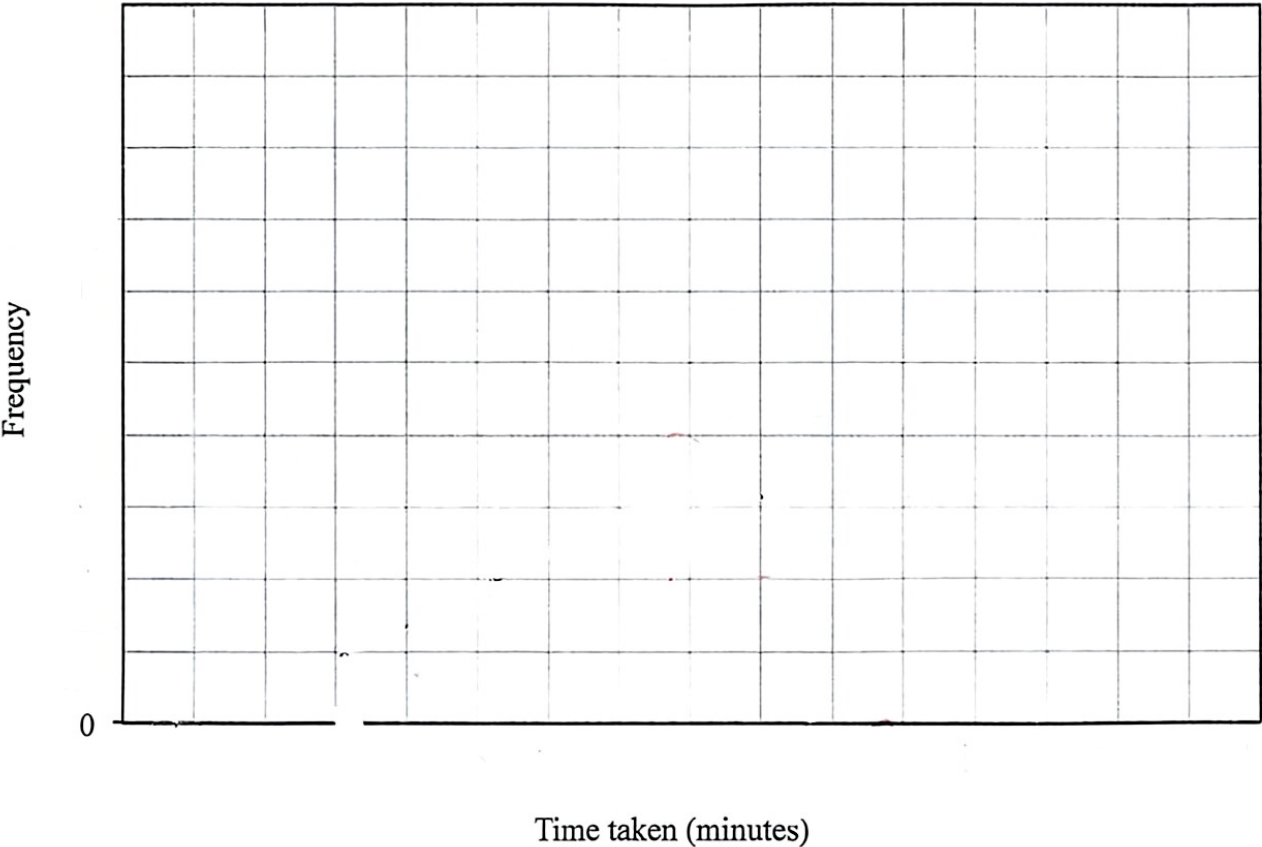
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(b) Draw the frequency polygon to present the data.

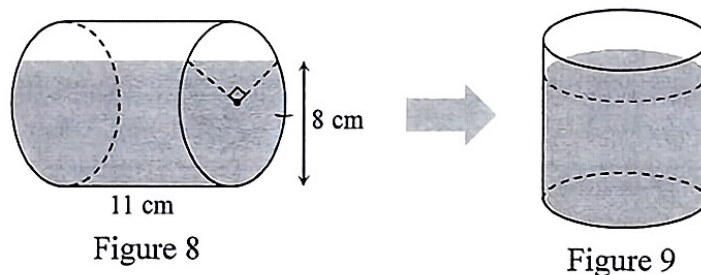
(3 marks)

**The time taken to finish an assignment by a group of students**





16. A right cylindrical sealed container of height 11 cm is placed horizontally on a table as shown in Figure 8. The water level in the container is 8 cm above the table.



- (a) Find the base area of the water in the container in Figure 8.
- (b) The container is then placed vertically as shown in Figure 9. The volume of water in the container remains unchanged.
  - (i) Find the new water level.
  - (ii) Find the wet curved surface area of the container in Figure 9.

(8 marks)

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**Multiple-choice Questions (20 marks)**

Each question carries 2 marks. Put ✓ in the correct boxes.

	18	19	20	21	22	23	24	25	26	27
A										
B										
C										
D										

18. Which of the following are rational numbers?

I.  $\frac{3}{7}$

II.  $1.\dot{2}$

III.  $\sqrt{2}$

IV.  $\sqrt[3]{27}$

A. I and II only ✗

B. III and IV only

C. I, II and III only

D. I, II and IV only ✓

19. If  $p : q = 5 : 2$  and  $q : r = 1 : 3$ , then  $(2p - q) : (4q + 2r) =$ A.  $2 : 5$ .B.  $3 : 5$ .C.  $6 : 7$ . ✗D.  $9 : 7$ .20. If  $A$  and  $B$  are constants such that  $(x + 1)(x - 3) + A(x - 3) \equiv x^2 + Bx$ , then  $A =$ A.  $-3$ .B.  $-1$ .C.  $1$ .D.  $3$ .21. Solve the simultaneous equations  $2x - 2y = 7x + 2y = 18$ .A.  $x = 4, y = -5$ B.  $x = 4, y = 5$ C.  $x = -4, y = -5$ D.  $x = -4, y = 5$



22. The weight of a pack of candy is measured as 250 g, correct to the nearest 5 g. Find its relative error.
- A.  $\frac{1}{100}$
- B.  $\frac{1}{50}$
- C.  $\frac{1}{25}$
- D.  $\frac{2}{25}$
23. If the sum of interior angles of a regular  $n$ -sided polygon is 7 times the sum of its exterior angles, which of the following must be true?
- I. The value of  $n$  is 16.
- II. The size of each exterior angle of the polygon is  $25^\circ$ .
- III. The size of each interior angle of the polygon is  $157.5^\circ$ .
- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III

24. In Figure 11,  $\frac{AB}{CD} =$

- A.  $\frac{\sin \alpha}{\cos \beta}$ .
- B.  $\frac{\cos \alpha}{\sin \beta}$ .
- C.  $\sin \alpha \cos \beta$ .
- D.  $\cos \alpha \sin \beta$ .

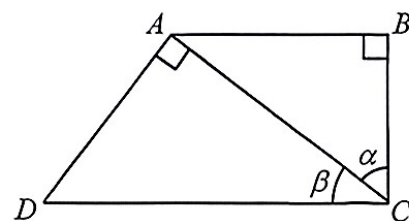


Figure 11

25. Figure 12 shows a cake composed of two right cylindrical layers. Find the total surface area of the cake.
- A.  $60\pi \text{ cm}^2$
- B.  $96\pi \text{ cm}^2$
- C.  $132\pi \text{ cm}^2$
- D.  $156\pi \text{ cm}^2$

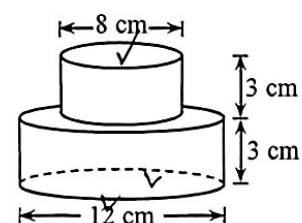


Figure 12

26. In Figure 13,  $PQRS$  is a rectangle.  $N$  is a point on  $QR$ .

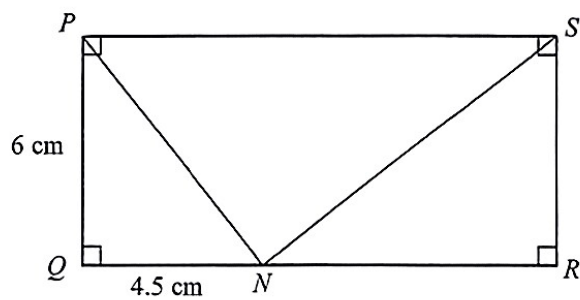


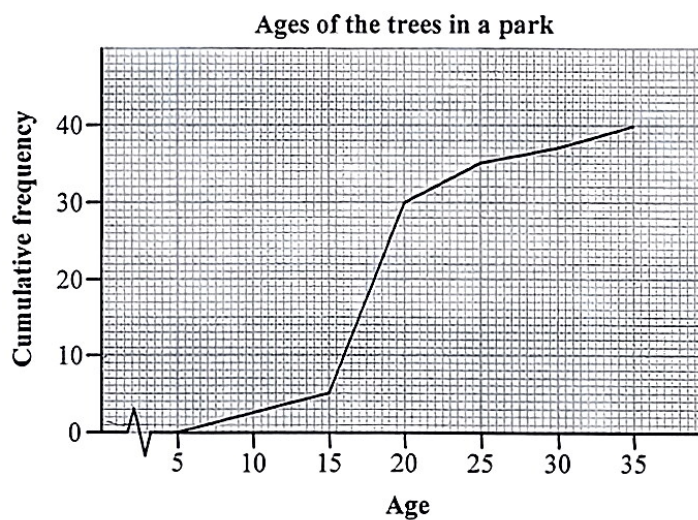
Figure 13

It is given that  $\triangle PQN \sim \triangle NRS$ . Which of the following are true?

- I.  $PN \perp NS$
- II.  $\triangle PQN \sim \triangle SNP$
- III.  $PS = 12.5$  cm

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III

27. The cumulative frequency polygon below shows the ages of the trees in a park.



The 80th percentile =

- A. 20
- B. 22
- C. 24
- D. 32

28. Simplify  $\sqrt{9-2\sqrt{23-6\sqrt{6-4\sqrt{2}}}}$ .

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