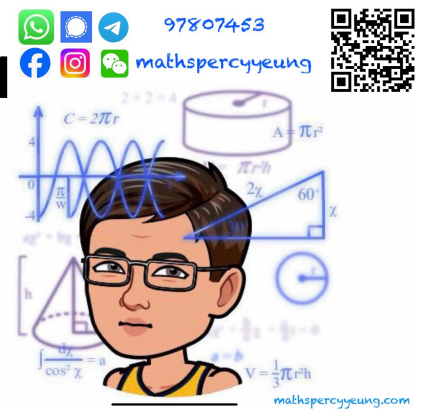


# SY 21-22 F.3 Maths Final Exam Paper 1



## Final Examination, 2021-2022 Mathematics Paper 1

Time allowed: 1.5 hours

Form 3

Full Marks: 100

- ◇ Answer ALL questions.
- ◇ Unless otherwise specified, all working must be clearly shown.
- ◇ The diagrams in this paper are not necessarily drawn to scale.
- ◇ Unless otherwise specified, numerical answers should either be exact or correct to 3 significant figures.

1. Simplify  $\frac{b^4}{(a^{-2}b)^3}$  and express your answer with positive indices.

(4 marks)

2. Factorize

(a)  $x^2 + 8x + 16$  ,

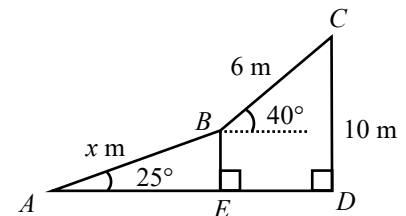
(b)  $x^2 - 3xy + 8x - 12y + 16$  .

(4 marks)

3. Mike deposited \$50000 at an interest rate 4% p.a. compounded half-yearly. Find the interest he will earn after 3 years. Correct your answer to the nearest dollar.

(4 marks)

4. In the figure,  $A$ ,  $E$  and  $D$  are the points on a horizontal ground.  $CD$  and  $BE$  are two vertical flag poles. It is given that  $AB = x$  m,  $BC = 6$  m and  $CD = 10$  m. If the angles of elevation from  $A$  to  $B$  and from  $B$  to  $C$  are  $25^\circ$  and  $40^\circ$  respectively, find  $x$ .



(3 marks)

5. If the distance between  $(-2, 0)$  and  $(a, 2a)$  is 10, find the two possible values of  $a$ .

(5 marks)

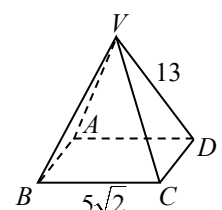
6. (a) Solve  $\frac{2x-1}{3} > 1 + \frac{x}{5}$  and represent your answer graphically.

(b) Hence solve  $\left( \frac{2x-1}{3} > 1 + \frac{x}{5} \text{ and } 2 \leq x \leq 5 \right)$  .

(6 marks)

7. In a right pyramid  $VABCD$ , the base  $ABCD$  is a square. It is given that  $VD = 13$  and  $BC = 5\sqrt{2}$ . Find the volume of  $VABCD$ .

(5 marks)



8. If one of the solutions of  $2x^2 + nx - 12 = 0$  is 4, where  $n$  is a constant, find

- (a)  $n$ ,  
(b) the other solution.

(5 marks)

9. The table below shows the number of siblings of the students in a class in January.

The number of siblings of a student	0	1	2	3
The number of students	3	13	5	4

- (a) Find the mean, median and mode of the number of siblings of students.  
(b) There will be  $n$  students with exactly 1 sibling withdraw in the next academic year. If the median and the mode do not change, write down the greatest possible value of  $n$ .  
(c) 5 students will join the class in the next month. With these students,  $w$  student(s) do not have sibling,  $x$  student(s) have 1 sibling,  $y$  student(s) have 2 siblings and  $z$  student(s) have 3 siblings. If the mean, median and mode do not change, write down a set of possible values of  $w$ ,  $x$ ,  $y$  and  $z$ .

(7 marks)

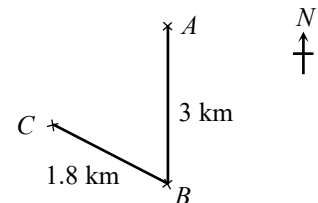
10. There are four balls in a bag, 2 red balls ( $R_1$  and  $R_2$ ), 1 blue ball ( $B$ ) and 1 green ball ( $G$ ). Two balls are drawn randomly from the bag one by one with replacement.

- (a) List out all possible outcomes by using a table.  
(b) Using (a), or otherwise, find the probability of getting 2 balls with the same colour.  
(c) Mark says if getting 2 balls at the same time, the probability of getting the same colour is the same as in (b). Do you agree? Explain your answer.

(6 marks)

11. A man rides a bicycle from  $A$  to  $B$ , where  $B$  is 3 km due south of  $A$ . Then he rides 1.8 km to  $C$  in the direction  $N60^\circ W$ .

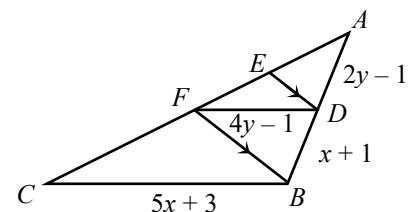
- (a) Find the true bearing of  $C$  from  $A$ .  
(b) Find  $AC$ .



(6 marks)

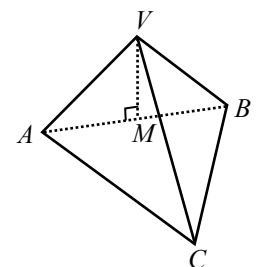
12. In the figure,  $F$  and  $E$  are the mid-points of  $AC$  and  $AB$  respectively. It is given that  $ED \parallel FB$ . Find the values of  $x$  and  $y$ .

(6 marks)



13. In the figure,  $VABC$  is a tetrahedron.  $M$  is the mid-point of  $AB$ . It is given that  $V$  is vertically above  $M$ .  $AB = BC = CA = 4$  and  $VA = VB = 3$ .

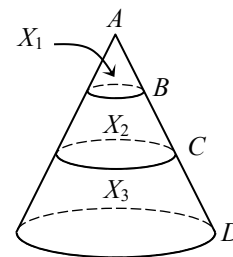
- (a) Find  $VM$ .  
(b) Find the angle between  $VC$  and plane  $ABC$ .



(6 marks)

14. In the figure, a right circular cone is divided into 3 parts ( $X_1$ ,  $X_2$  and  $X_3$ ) by two planes which are parallel to its base.  $AD$  is the slant height of the original cone, while  $B$  and  $C$  are the points on the slant height that are cut by the parallel planes. Let the curved surface areas of  $X_1$ ,  $X_2$  and  $X_3$  be  $S_1$ ,  $S_2$  and  $S_3$  respectively. It is given that  $S_1 : S_2 : S_3 = 1 : 8 : 27$ .

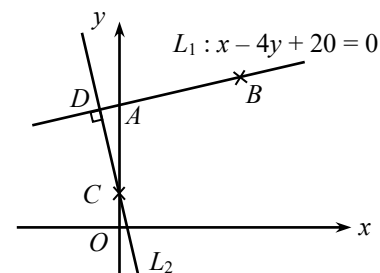
- (a) Find  $AB : AC : AD$ .  
 (b) If the volume of  $X_2$  is  $78 \text{ cm}^3$ , find the volume of the original cone.



(6 marks)

15. In the figure,  $L_1 : x - 4y + 20 = 0$  passes through  $B$  and cuts the  $y$ -axis at  $A$ . The  $x$ -coordinate of  $B$  is 4.

- (a) Find the coordinates of  $A$ .  
 (b)  $C$  is a point on  $OA$  such that  $OC : CA = 2 : 3$ .  $L_2$  passes through  $C$  and intersects  $L_1$  at  $D$ . It is given that  $L_2 \perp L_1$ .  
 (i) Write down the coordinates of  $C$ .  
 (ii) Find the equation of  $L_2$ .  
 (iii) Find the coordinates of  $D$ .  
 (iv) Find the area of  $\triangle BCD$ .

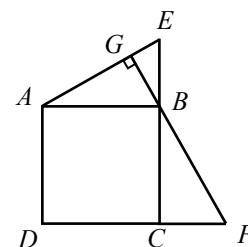


(11 marks)

16. In the figure,  $ABCD$  is a square.  $CBE$ ,  $DCF$  and  $FBG$  are straight lines. It is given that  $AE \perp GF$ .

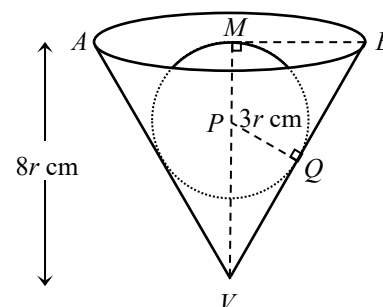
- (a) Prove that  $\triangle ABE \cong \triangle BCF$ .  
 (b) If  $DF = 23$  and  $AE = 17$ , find  $DC$ .

(7 marks)



17. In the figure, an inverted right circular conical container  $VAB$  contains some water inside it. When a sphere is put into it, a point  $M$ , which is the centre of the base circle of the container, lies on the surface of the sphere. The radius  $PQ$  of the sphere is  $3r \text{ cm}$  and the height of the container is  $8r \text{ cm}$ .

- (a) Find  $VQ$  and  $MB$  in terms of  $r$ .  
 (b) If there are  $240\pi \text{ cm}^3$  of water in the container and the water level reaches the base circle without overflow, find  $r$ .



(9 marks)

~ End of Paper ~