

# Equation of Straight Lines

## Multiple Choice Question

[19-20]

## 1. [19-20 Mid-year, #7]

Find the equation of the straight line with slope  $-\frac{1}{2}$  and  $x$ -intercept 5.

- A.  $x + 2y - 10 = 0$       B.  $x + 2y + 10 = 0$   
 C.  $x + 2y - 5 = 0$       D.  $x + 2y + 5 = 0$

## 2. [19-20 Mid-year, #20]

The area enclosed by the straight lines  $4x + 7y + 84 = 0$ , the  $y$ -axis and  $y = -4$  is

- A. 56 square units.  
 B. 112 square units.  
 C. 126 square units.  
 D. 252 square units.

[20-21]

## 3. [20-21 S4 Standardized Test #3]

Find the constant  $k$  such that the straight lines  $x + 2y + k = 0$  and  $kx - 3y + 5 = 0$  are perpendicular to each other.

- A. 12  
 B. 6  
 C. -6  
 D. -12

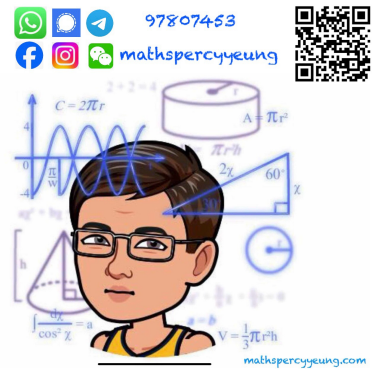
## 4. [20-21 S4 Standardized Test #4]

It is given that  $\begin{cases} L_1 : 2x + y + 3 = 0 \\ L_2 : x - 2y - 1 = 0 \end{cases}$ . Denote the point of intersection of  $L_1$  and  $L_2$  by  $A$ . Find the equation of the straight line which passes through the origin and  $A$ .

- A.  $x - y = 0$   
 B.  $x + y = 0$   
 C.  $x - 2y = 0$   
 D.  $2x + y = 0$

## 5. [20-21 S4 Standardized Test #5]

The straight line  $L$  is parallel to the straight line  $4x - 2y + 1 = 0$ . If the  $x$ -intercept of  $L$  is 5, then the equation of  $L$  is



## Equation of Straight Lines

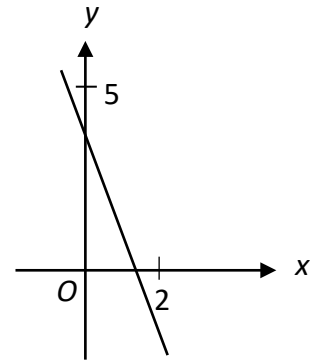
- A.  $2x - y + 5 = 0$ .
- B.  $2x - y - 10 = 0$ .
- C.  $x - 2y + 10 = 0$ .
- D.  $x + 2y - 5 = 0$ .

## 6. [20-21 S4 Standardized Test #8]

In the figure, the equation of the straight line  $L$  is  $ax - by + 10 = 0$ . Which of the following must be correct?

- I.  $a > -5$
- II.  $b > 2$
- III.  $a < b$

- A. I only
- B. II only
- C. I and III only
- D. II and III only



7. [20-21 S5 Mid-year #5]

The equation of the straight line  $L$  is  $3x + 4y + 2 = 0$ . The equation of the straight line passing through  $(3, -5)$  and perpendicular to  $L$  is

- A.  $4x + 3y - 3 = 0$ .
- B.  $4x - 3y - 27 = 0$ .
- C.  $3x + 4y - 3 = 0$ .
- D.  $3x - 4y - 27 = 0$ .

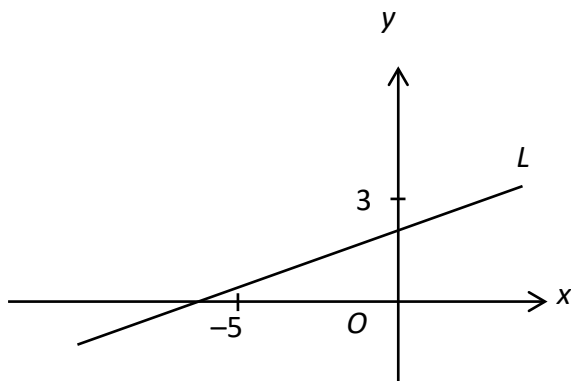
8. [20-21 Final Exam, #13]

The coordinates of points  $A$ ,  $B$  and  $C$  are  $(3, 3)$ ,  $(1, -2)$  and  $(-3, 4)$  respectively. Let  $P$  be the mid-point of  $BC$ . Find the equation of  $AP$ .

- A.  $x - 2y + 3 = 0$
- B.  $3x + 2y + 1 = 0$
- C.  $7x + 10y - 19 = 0$
- D.  $11x + 2y - 7 = 0$

9. [20-21 Final Exam, #25]

In the figure, the equation of the straight line  $L$  is  $x + ay = b$ . Which of the following is/are true?



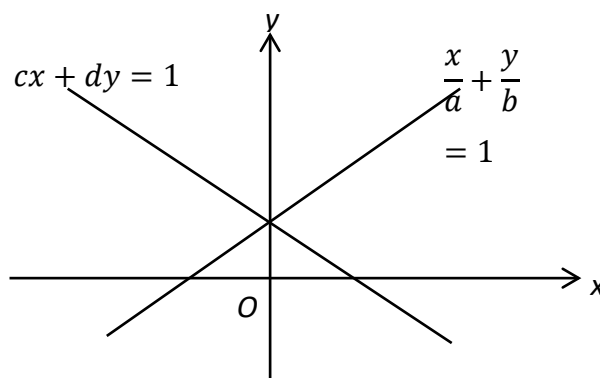
- I.  $a < 0$
  - II.  $b < 3a$
  - III.  $b < -5$
- 
- A. I only
  - B. II only
  - C. I and III only
  - D. II and III only

## Equation of Straight Lines

## 10. [20-21 Final Exam, #26]

In the figure, the two straight lines intersect at a point on the positive  $y$ -axis. Which of the following are true?

- I.  $a < 0$
  - II.  $c < 0$
  - III.  $bd = 1$
- A. I and II only
  - B. I and III only
  - C. II and III only
  - D. I, II and III

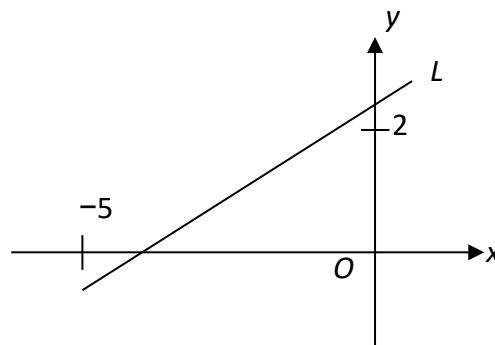


## 11. [20-21 S.5 Final Exam, #18]

In the figure, the equation of the straight line  $L$  is  $x + by + c = 0$ . Which of the following are true?

- I.  $0 < c < 5$
- II.  $-2.5 < b < 0$
- III.  $c > -2b$

- I and II only
- I and III only
- II and III only
- I, II and III



## [21-22]

## 12. [21-22 Final Exam, #8]

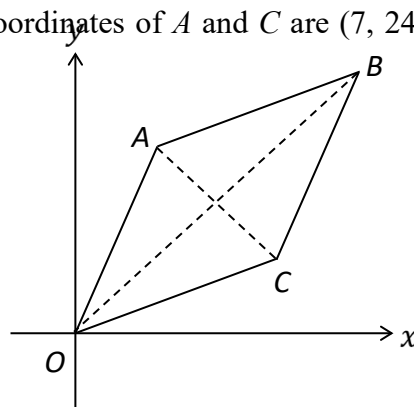
The slope of the straight line  $L$ :  $(m + 10)x - my - 20 = 0$  is  $-4$ . Find the  $y$ -intercept of  $L$ .

- A.  $-10$
- B.  $-2.5$
- C.  $2.5$
- D.  $10$

13. [21-22 Final Exam, #9]

In the figure,  $O$  is the origin and  $OABC$  is a rhombus. The coordinates of  $A$  and  $C$  are  $(7, 24)$  and  $(20, 15)$  respectively. Find the equation of  $OB$ .

- A.  $2x - y = 0$
- B.  $9x - 13y = 0$
- C.  $13x - 9y = 0$
- D.  $9x + 13y = 0$



14. [21-22 Final Exam, #19]

The straight line  $7x - 24y + 168 = 0$  cuts the  $x$ -axis and the  $y$ -axis at  $A$  and  $B$  respectively. If  $O$  is the origin and  $P$  is a point on  $AB$  such that  $OP \perp AB$ , then  $OP =$

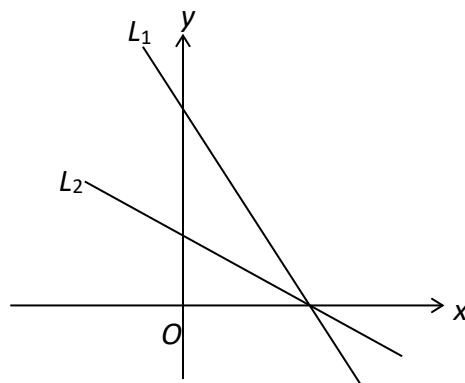
- A. 6.72 .
- B. 7.16 .
- C. 7.28 .
- D. 8.24 .

15. [21-22 Final Exam, #24]

In the figure, the equations of straight lines  $L_1$  and  $L_2$  are  $y = \frac{2x+b}{a}$  and  $y = \frac{cx-d}{2}$  respectively.  $L_1$  and  $L_2$  intersect at a point on the positive  $x$ -axis. Which of the following are true?

- I.  $c < 0$
- II.  $bc - 2d = 0$
- III.  $ac < 4$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III



## Equation of Straight Lines

## 16. [21-22 S.5 Mid-year, #8]

Find the constant  $k$  such that the straight lines  $kx + 4y + 8 = 0$  and  $4x - 8y - k = 0$  are perpendicular to each other.

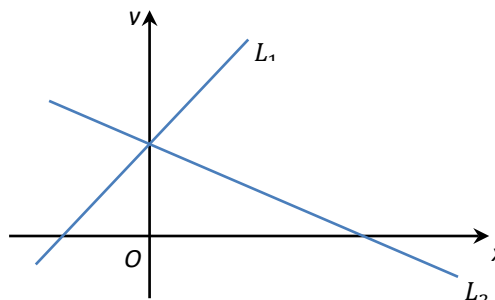
- A.  $-8$
- B.  $-2$
- C.  $2$
- D.  $8$

## 17. [21-22 S.5 Mid-year, #17]

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $ax + 2by = 1$  and  $3cx + 4y = d$  respectively.  $L_1$  and  $L_2$  intersect at a point on the positive  $y$ -axis. Which of the following are true?

- I.  $bd = 2$
- II.  $a < \frac{3}{2}bc$
- III.  $ad > 3c$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III

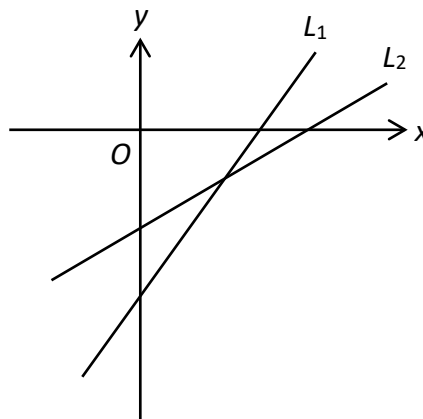


## 18. [21-22 S.5 Mid-year, #22]

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $2x + ay = b$  and  $cx - 5y = 3b$  respectively. Which of the following are true?

- I.  $b > 0$
- II.  $c > a$
- III.  $ac > -10$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III



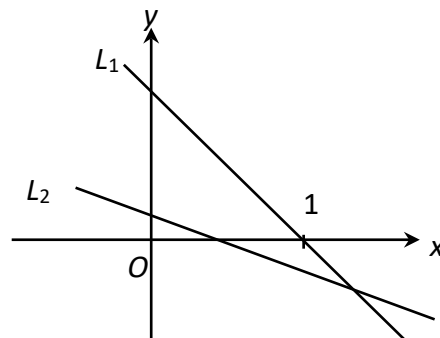
## Equation of Straight Lines

## 19. [21-22 S.6 Standardized Test, #7]

The figure shows the straight lines  $L_1: y + ax = b$  and  $L_2: y + cx = d$ . Which of the following are true?

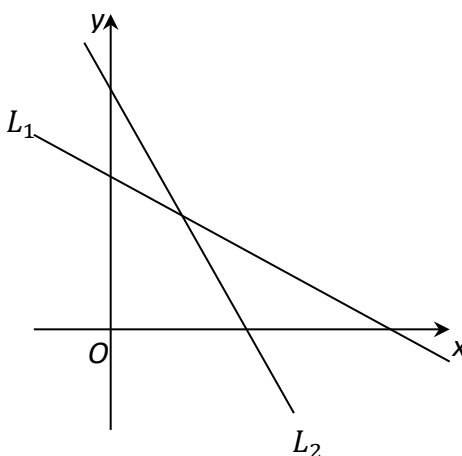
- I.  $a > c > 0$
- II.  $b > d$
- III.  $c > d$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III



## 20. [21-22 S.6 Mock, #7]

In the figure, the equations of the straight line  $L_1$  and  $L_2$  are  $x - ay - b = 0$  and  $x - cy - d = 0$  respectively. Which of the following are true?



- I.  $a > c$
- II.  $b > d$
- III.  $bc > ad$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III

## Equation of Straight Lines

## 21. [21-22 S.6 Mock, #25]

Let  $k$  be a constant. The equations of straight lines  $L_1$  and  $L_2$  are  $kx - 2y + 15 = 0$  and  $kx + 8y - 3 = 0$  respectively. If  $L_1 \perp L_2$ , find the difference between the  $x$ -intercepts of  $L_1$  and  $L_2$ .

- A. 1.5
- B. 4.5
- C. 6.5
- D. 10.5

## 22. [21-22 S.6 Mock, #41]

The equations of the three sides of a triangle are  $ax - 6y + 6a = 0$ ,  $ax + 6y - 6a = 0$  and  $y = 0$ , where  $a$  is a positive constant. If the  $y$ -coordinate of the in-centre of the triangle is 3, then  $a =$

- A. 6
- B. 8
- C. 10
- D. 12

## [22-23]

## 23. [S.4 22-23 Mid-Year, #11]

The equation of the straight line  $L$  is  $ax - 18y - 5a = 0$ , where  $a$  is a constant. If  $L$  is perpendicular to the straight line  $9x + 4y = 0$ , find the  $y$ -intercept of  $L$ .

- A. -5
- B.  $-\frac{20}{9}$
- C.  $\frac{20}{9}$
- D. 5

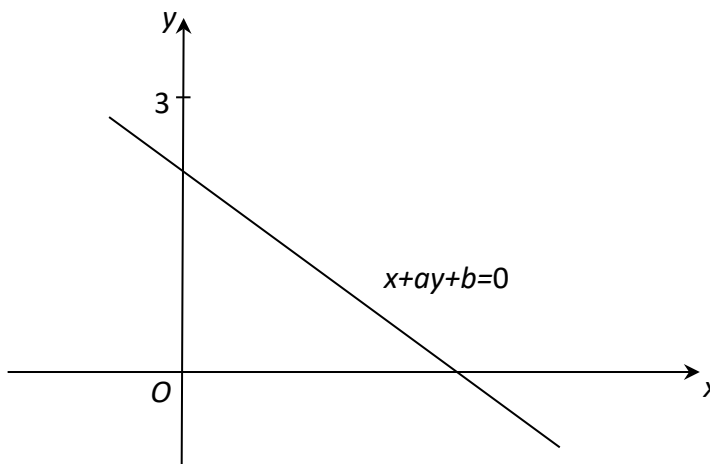
## Equation of Straight Lines

## 24. [S.4 22-23 Mid-Year,#20]

The figure shows the graph of the straight line  $x + ay + b = 0$ . Which of the following are true?

- I.  $a > 0$
- II.  $b < 0$
- III.  $3a + b > 0$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III



## 25. [S.4 22-23 Mid-Year,#21]

Consider two straight lines  $L_1: 2x - 7y - 7 = 0$  and  $L_2: 7x + 2y + 2 = 0$ . Which of the following must be true?

- I.  $L_1$  and  $L_2$  have no intersections.
- II.  $L_1 \perp L_2$
- III.  $L_1$  and  $L_2$  have the same x-intercept.

- A. I only
- B. II only
- C. I and III only
- D. II and III only

## 26. [S.4 22-23 Mid-Year,#22]

The equation of the straight line  $L$  is  $y = \frac{1}{4}x + 3$ .  $L$  intersects the x-axis and straight line  $x = 8$  at  $A$  and  $B$  respectively. The straight line  $x = 8$  intersects the x-axis at  $C$ . Find the area of  $\triangle ABC$ .

- A. 18 sq. units
- B. 36 sq. units
- C. 50 sq. units
- D. 100 sq. units

## 27. [S.4 22-23 Final,#5]

## Equation of Straight Lines

If the straight lines  $hx - 3y + 2 = 0$  and  $4x + 6y - 5 = 0$  are parallel, then  $h =$

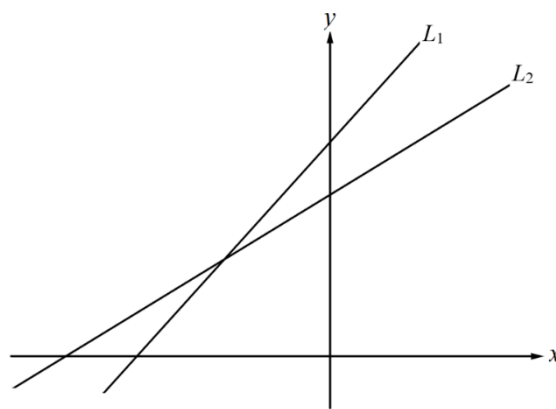
- A.  $-4$ .
- B.  $-2$ .
- C.  $2$ .
- D.  $4$ .

## 28. [S.4 22-23 Final,#22]

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $ax + by + 1 = 0$  and  $cx + dy + 1 = 0$  respectively. Which of the following must be true?

- I.  $a > c$
- II.  $b > d$
- III.  $ad < bc$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III

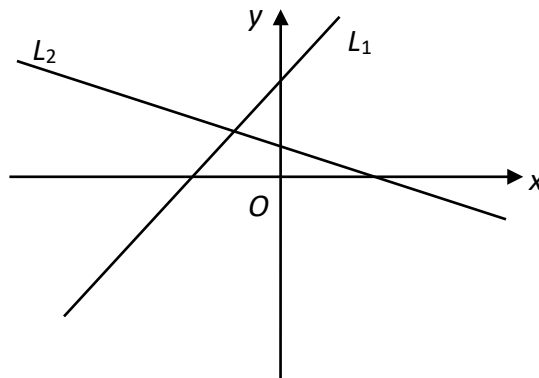


## 29. [S.5 22-23 Mid-year,#9]

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $x + ay = -1$  and  $y = -bx + c$  respectively. Which of the following are true?

- I.  $a < 0$
- II.  $b > 0$
- III.  $a(b + c) > 2$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III



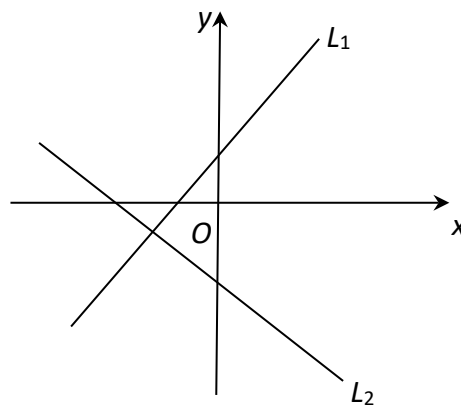
## 30. [S.5 22-23 Final,#19]

## Equation of Straight Lines

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $ax + y - b = 0$  and  $x + cy - d = 0$  respectively. Which of the following are true?

- I.  $c > 0$
- II.  $ad > b$
- III.  $d > bc$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III

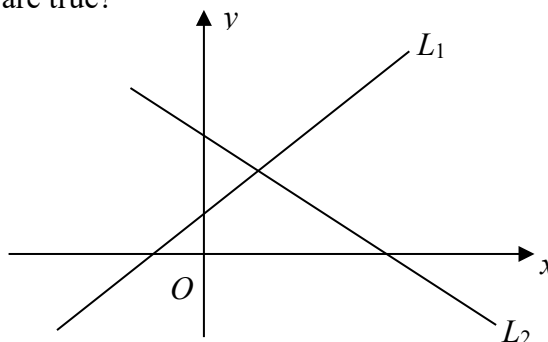


## 31. [S.6 22-23 Standardized Test,#4]

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $ax - y + b = 0$  and  $cx - y + d = 0$  respectively. Which of the following are true?

- I.  $c < 0$
- II.  $bd > 0$
- III.  $ad > bc$

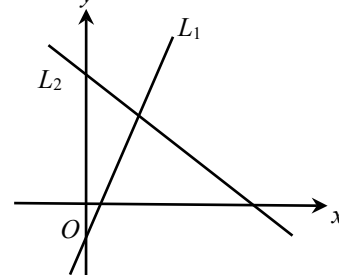
- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III



## 32. [S.6 22-23 Timed Practice 2,#11]

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $3x + ay - b = 0$  and  $cx + y + d = 0$  respectively, where  $a, b, c$  and  $d$  are constants. Which of the following must be true?

- I.  $a < 0$
  - II.  $d > 0$
  - III.  $bc + 3d < 0$
- A. I and II only
  - B. I and III only
  - C. II and III only
  - D. I, II and III



## 33. [S.6 22-23 Timed Practice 4,#24]

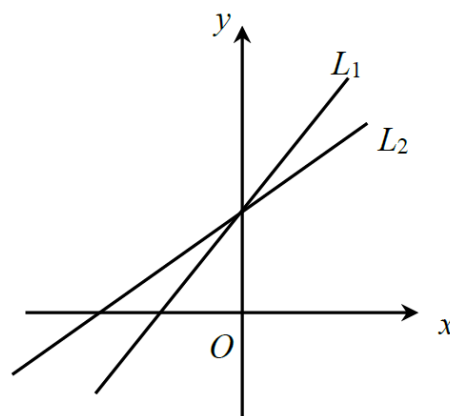
In the figure, the equation of  $L_1$  is  $x + ay + b = 0$  and the equation of  $L_2$  is  $x + cy + d = 0$ .

## Equation of Straight Lines

$L_1$  and  $L_2$  intersect at a point on the positive  $y$ -axis. Which of the following are true?

- I.  $a < 0$
- II.  $b > d$
- III.  $ad = bc$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III

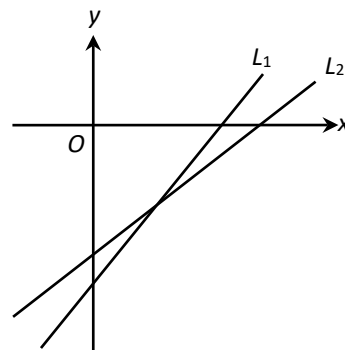


## 34. [S.6 22-23 Timed Practice 5,#26]

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $ax + 2y + b = 0$  and  $cx + y + d = 0$  respectively. Which of the following is/are true?

- I.  $a > 2c$
- II.  $b > 2d$
- III.  $ad > bc$

- A. I only
- B. II only
- C. I and III only
- D. II and III only

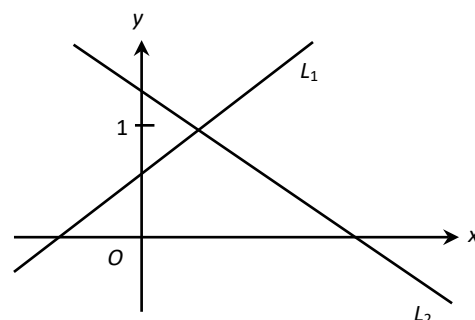


## 35. [S.6 22-23 Timed Practice 6,#10]

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $x + ay + b = 0$  and  $x + my + n = 0$  respectively. Which of the following are true?

- I.  $m + n < 0$
- II.  $a + b < 0$
- III.  $m < a$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III



## 36. [S.6 22-23 Timed Practice 6,#25]

The equations of the straight lines  $L_1$  and  $L_2$  are  $3x + hy - 20 = 0$  and  $kx + 8y + 15 = 0$  respectively,

## Equation of Straight Lines

where  $h$  and  $k$  are constants. If  $L_1$  is parallel to  $L_2$  and the  $y$ -intercept of  $L_1$  is  $-5$ , then  $k =$

- A.  $-6$ .
- B.  $-4$ .
- C.  $4$ .
- D.  $6$ .

## 37. [S.6 22-23 Timed Practice 6,#40]

The equation of the straight line  $L$  is  $4x + 3y - 3k = 0$ , where  $k$  is a positive constant.  $L$  cuts the  $x$ -axis and the  $y$ -axis at the points  $P$  and  $Q$  respectively. Let  $R$  be a point lying on the  $x$ -axis such that the  $y$ -coordinate of the orthocentre of  $\triangle PQR$  is 9. Find the  $x$ -coordinate of  $R$ .

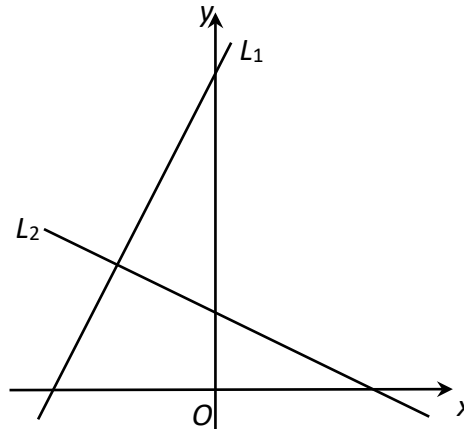
- A.  $-12$
- B.  $-3$
- C.  $3$
- D.  $12$

## 38. [22-23 S6 Mock,#7]

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $ax - y + b = 0$  and  $x + ay + c = 0$  respectively. Which of the following are true?

- I.  $a > 0$
- II.  $ac < b$
- III.  $ab + c > 0$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III



## 39. [22-23 S6 Mock,#25]

The straight line  $L$  is perpendicular to the straight line  $2x - 3y + 4 = 0$ . If the  $x$ -intercept of  $L$  is 5, then the equation of  $L$  is

- A.  $3x + 2y - 15 = 0$ .
- B.  $3x + 2y - 10 = 0$ .
- C.  $2x - 3y - 15 = 0$ .
- D.  $2x - 3y - 10 = 0$ .

[23-24]

40. [S.4 23-24 Mid-Year,#7]

The equation of the straight line  $L_1$  is  $2x + 3y + 6 = 0$ . If  $L_2$  is a straight line that is parallel to  $L_1$  and passes through  $(2, 8)$ , then the equation of  $L_2$  is

- A.  $2x + 3y - 28 = 0$ .
- B.  $2x + 3y + 28 = 0$ .
- C.  $3x + 2y - 22 = 0$ .
- D.  $3x + 2y + 22 = 0$ .

41. [S.4 23-24 Mid-Year,#8]

If the straight lines  $hx + 9y - 2 = 0$  and  $4x + ky + 5 = 0$  do not intersect, which of the following can be the values of  $h$  and  $k$ ?

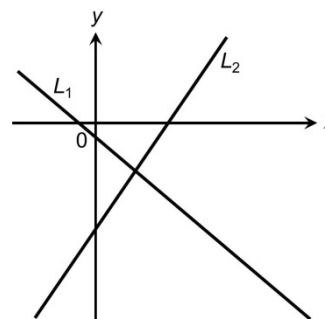
- A.  $h = -3, k = 12$
- B.  $h = 3, k = 15$
- C.  $h = 12, k = 3$
- D.  $h = 16, k = 3$

42. [S.4 23-24 Mid-Year,#19]

The figure shows two straight lines  $L_1 : ax + by = 1$  and  $L_2 : cx + dy = 1$ . Which of the following must be true?

- I.  $a < 0$
- II.  $b > d$
- III.  $bc < ad$

- A. I and III only
- B. I and II only
- C. II and III only
- D. I, II and III



43. [S.4 23-24 Final,#5]

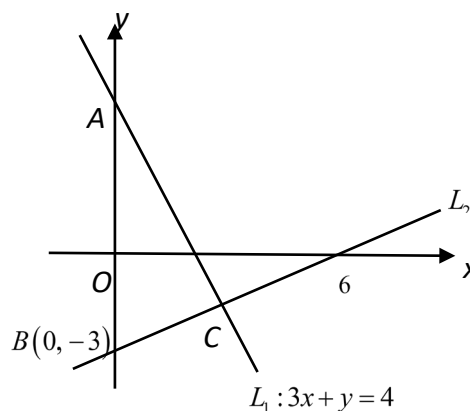
If the straight lines  $3x - 2y + 5 = 0$  and  $kx + 21y - 9 = 0$  are perpendicular to each other, then  $k =$

- A. 6.
- B. 12.
- C. 14.
- D. 21.

44. [S.4 23-24 Final,#15]

In the figure,  $L_1 : 3x + y = 4$  cuts the  $y$ -axis at  $A$ .  $L_2$  is another straight line passing through  $B(0, -3)$  and cuts the  $x$ -axis at  $(6, 0)$ . Denote the point of intersection of  $L_1$  and  $L_2$  by  $C$ . Find the area of  $\triangle ABC$ .

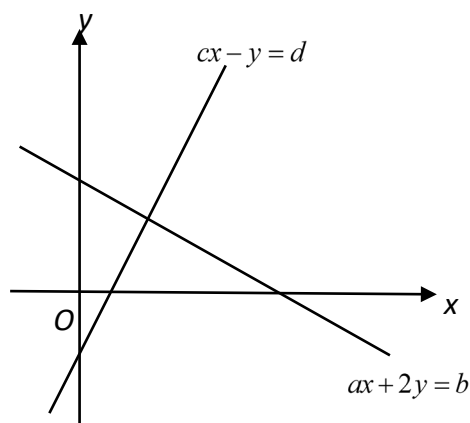
- A. 6
- B. 7
- C. 12
- D. 14



45. [S.4 23-24 Final,#16]

The figure shows the straight lines  $ax + 2y = b$  and  $cx - y = d$ . Which of the following must be true?

- I.  $c > 0$
  - II.  $b + 2d > 0$
  - III.  $ad - bc > 0$
- 
- A. I and II only
  - B. I and III only
  - C. II and III only
  - D. I, II and III



## Equation of Straight Lines

## 46. [S.5 23-24 Mid-year,#21]

If the straight lines  $x + ay = 3$  and  $x - 2y = b$  are perpendicular to each other and intersect at a point on the  $y$ -axis, then  $b =$

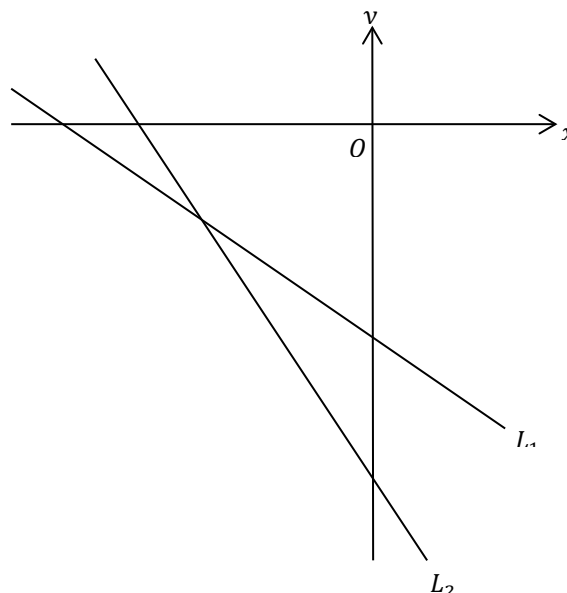
- A.  $-12$ .
- B.  $-2$ .
- C.  $\frac{1}{2}$ .
- D.  $6$ .

## 47. [S.5 23-24 Mid-year,#22]

In the figure, the equations of the straight lines  $L_1$  and  $L_2$  are  $px + qy = 4$  and  $mx + ny = 8$  respectively. Which of the following are true?

- I.  $pn < mq$
- II.  $n < 2q$
- III.  $m < 2p$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III



## 48. [S.5 23-24 Final,#25]

Let  $a$  be a constant. Find the possible values of  $a$  such that the straight lines  $3x + \left(\frac{a}{2}\right)y - 7 = 0$  and  $4x - (a + 2)y + 3 = 0$  are perpendicular to each other.

- A.  $6$
- B.  $\frac{6}{5}$
- C.  $-4$  or  $6$
- D.  $-6$  or  $4$

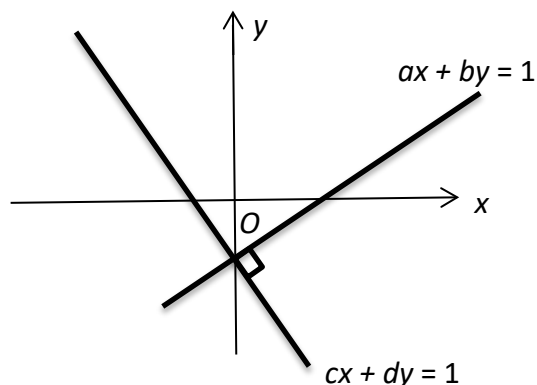
## 49. [S.5 23-24 Final,#26]

## Equation of Straight Lines

In the figure, the two perpendicular straight lines intersect at a point on the negative  $y$ -axis.  
Which of the following are true?

- I.  $b < 0$ .
- II.  $a < c$ .
- III.  $d^2 + ac = 0$ .

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III

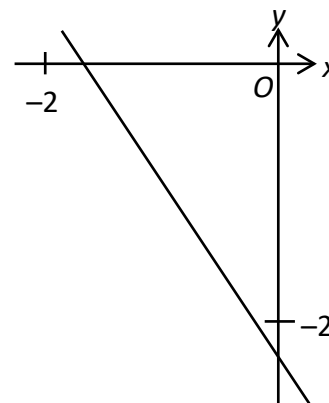


## 50. [S.6 23-24 Standardized Test, #12]

The figure shows the graph of the straight line  $ax + by + 24 = 0$ . Which of the following are true?

- I.  $b < 12$
- II.  $a > 12$
- III.  $a = b$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III



## 51. [S.6 23-24 Timed Practice 2, #22]

$$\frac{1}{5+6x} + \frac{2}{5-6x} =$$

- A.  $\frac{15+6x}{25-36x^2}$
- B.  $\frac{15-6x}{25-36x^2}$
- C.  $\frac{15-18x}{25-36x^2}$
- D.  $\frac{15}{25-36x^2}$

## 52. [S.6 23-24 Timed Practice 2, #35]

The equations of the straight lines  $L_1$  and  $L_2$  are  $5x - 2y + k = 0$  and  $2x + 5y - k = 0$  respectively, where  $k$  is a positive constant. It is given that  $L_1$  cuts the  $y$ -axis at the point  $A$ . Denote the point of intersection of  $L_1$  and  $L_2$  by  $B$ . If  $C$  is a point lying on  $L_2$  such that the in-centre of  $\triangle ABC$  lies on the  $y$ -axis, then the  $y$ -coordinate of  $C$  is

- A.  $\frac{k}{7}$
- B.  $2k$
- C.  $5k$
- D.  $7k$

**53. [S.6 23-24 Timed Practice 4,#22]**

A straight line  $L_1$  has the same  $y$ -intercept as the straight line  $L_2 : 3x - 5y - 15 = 0$  and  $L_1$  is perpendicular to  $L_2$ . Find the equation of  $L_1$ .

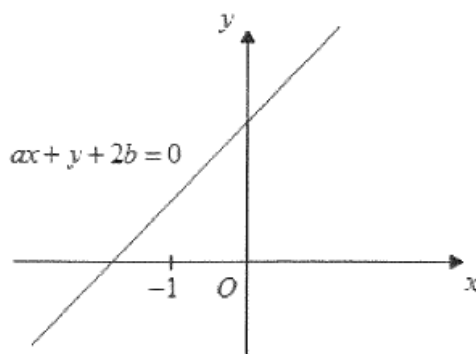
- A.  $3x + 5y + 15 = 0$
- B.  $3x - 5y - 15 = 0$
- C.  $5x + 3y + 9 = 0$
- D.  $5x + 3y - 9 = 0$

**54. [S.6 23-24 Timed Practice 6,#24]**

The figure shows the graph of the straight line  $ax + y + 2b = 0$ . Which of the following are true?

- I.  $a < 0$
- II.  $b < 0$
- III.  $\frac{a}{2} < b$

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II and III



~End~

## Equation of Straight Lines Conventional Questions

[19-20]

1. [S.4 19-20 Mid-year, #13]

In **Figure 1**, two straight lines  $L_1$  and  $L_2$  cut the  $x$ -axis at  $B$  and the origin respectively.  $A$  is the point of intersection of  $L_1$  and  $L_2$ .  $C$  is a point on  $AB$  such that  $OC$  is the median of  $AB$  in  $\triangle AOB$ . It is given that the equation of  $L_1$  is  $x + y - 6 = 0$  and the coordinates of  $A$  are  $(-3, 9)$ .

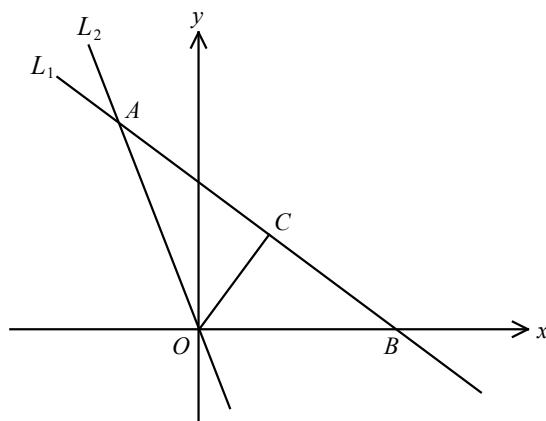


Figure 1

- (a) Write down the coordinates of  $B$ . (1 mark)
- (b) Find the equation of  $OC$ . (3 marks)

2. [S.4 20-21 Standardized Test, #3]

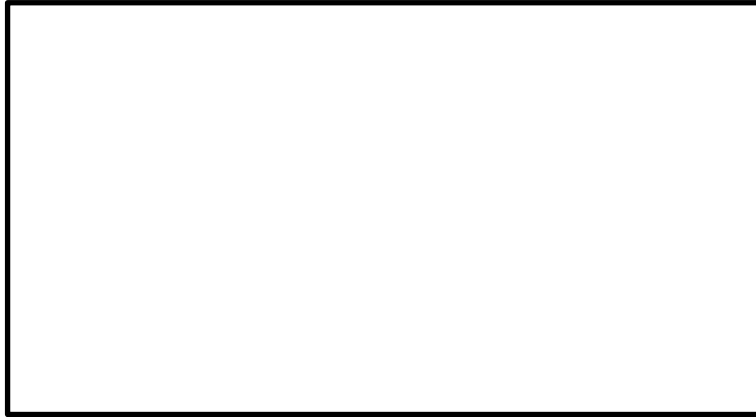
It is given that the straight line  $L_1$  passes through  $A(3, -7)$  and  $B(1, 5)$ .

- (a) Find the equation of  $L_1$ . (2 marks)
- (b) The straight line  $L_2$  passes through  $C(4, -9)$  and it is perpendicular to  $L_1$ . Find the equation of  $L_2$ . (2 marks)

3. [S.4 20-21 Standardized Test, #4]

The straight line  $L: 2x - y - 8 = 0$  cuts the  $x$ -axis and the  $y$ -axis at  $A$  and  $B$  respectively.

- (a) Write down the coordinates of  $A$  and  $B$ . **(2 marks)**
- (b) It is given that the perpendicular bisector of  $AB$  intersects  $L$  at  $M$  and cuts the  $x$ -axis at  $C$ .
- (i) Sketch the graph of  $L$  and the perpendicular bisector of  $AB$  in the box provided.
- (ii) Find the equation of the perpendicular bisector of  $AB$ .
- (iii) Write down the equation of the straight line parallel to the  $y$ -axis and passes through  $C$ . **(5 marks)**



4. [S.4 20-21 Final Exam, #6]

The coordinates of the points  $A$  and  $B$  are  $(-2, 0)$  and  $(6, 12)$  respectively. The straight line  $L_1$  passes through  $A$  and  $B$ .

- (a) Find the equation of  $L_1$ .
- (b) The slope of another straight line  $L_2$  is  $-\frac{12}{5}$ . If  $L_2$  passes through  $B$ , find the equation of  $L_2$ . **(4 marks)**

5. [S.4 20-21 Final Exam, #16]

In **Figure 1**, the coordinates of  $A$  and  $C$  are  $(-8, 12)$  and  $(0, -4)$  respectively.  $L_1$  is the perpendicular bisector of  $AC$  and it cuts  $AC$  and the  $y$ -axis at  $M$  and  $B$  respectively.

- (a) Find the coordinates of  $M$ . (1 mark)
- (b) Find the equation of  $L_1$ . (3 marks)
- (c)  $L_2$  is a straight line passes through  $A$ . It is given that the equation of  $L_2$  is  $y = -\frac{5}{4}x + 2$  and it cuts  $L_1$  at  $N$ .
  - (i) Find the coordinates of  $N$ .
  - (ii) Find the ratio of the area of  $\triangle ABM$  to the area of  $\triangle ABN$ .

(4 marks)

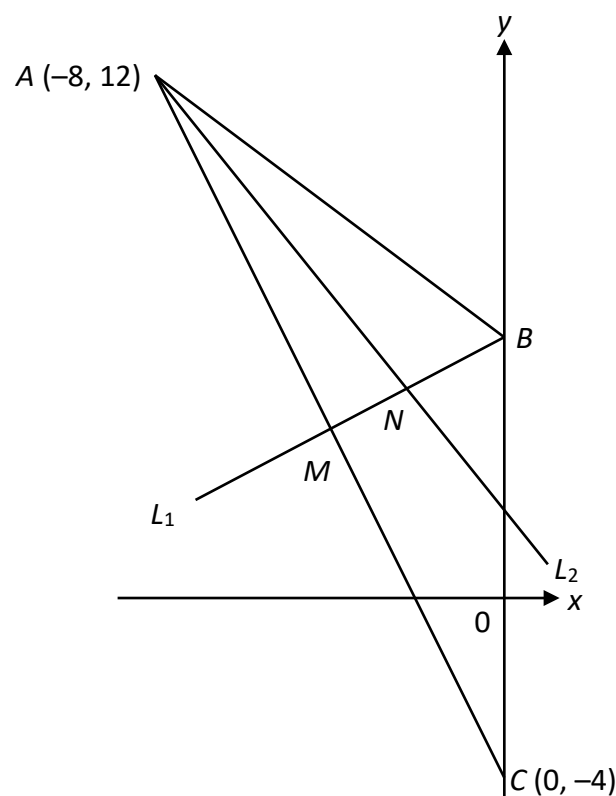


Figure 1

[21-22]

6. [S.4 21-22 Final, #6]

The slope of the straight line  $L_1$  is  $\frac{1}{3}$ . The straight line  $L_2$  passes through  $A(-2, 5)$  and  $L_1$  does not intersect with  $L_2$ .

- (a) Find the equation of  $L_2$  in the general form.
  - (b) If  $L_2$  passes through  $P(4, k)$ , find the equation of the horizontal line passing through  $P$ .
- (5 marks)

7. [S.4 21-22 Final, #13]

The straight line  $L_1: x + 2y - 10 = 0$  cuts the  $x$ -axis and the  $y$ -axis at  $A$  and  $B$  respectively. Another straight line  $L_2$  passes through  $A$  and is perpendicular to  $L_1$ .  $L_2$  cuts the  $y$ -axis at  $C$ . Denote the origin by  $O$ .

- (a) Find the equation of  $L_2$ . (2 marks)
- (b) Suppose  $P$  is a point lying on  $L_2$  and above the  $x$ -axis such that  $\angle POA = 45^\circ$ . It is given that the  $x$ -coordinate of  $P$  is  $h$ .
- (i) Find  $h$ .
- (ii) Find the distance between the orthocenter of  $\triangle ABC$  and  $P$ . Give your answer in surd form if necessary. (4 marks)

8. [S.5 21-22 Mid-year, #5]

The straight line  $L: 5x + 3y - 30 = 0$  cuts the  $x$ -axis and the  $y$ -axis at  $A$  and  $B$  respectively.

- (a) Write down the coordinates of  $A$  and  $B$ .
- (b) Find the equation of the perpendicular bisector of  $AB$ . (4 marks)

9. [S.5 21-22 Mid-year, #18]

Let  $C$  be the graph of  $y = 2x^2 - 12kx + 32k^2 + 6$ , where  $k$  is a real constant.

- (a) Using the method of completing the square, express the coordinates of the vertex of  $C$  in terms of  $k$ . (3 marks)
- (b) Let  $L$  be a straight line with slope  $4k$ . Someone claims that if  $y$ -intercept of  $L$  is negative, then  $L$  and  $C$  must not intersect. Do you agree? Explain your answer. (3 marks)

10. [S.6 21-22 Standardized Test, #7]

The straight lines  $L_1$  and  $L_2$  are perpendicular to each other. The  $x$ -intercept of  $L_1$  is 8. It is given that  $L_1$  and  $L_2$  intersect at the point  $(5, 2)$ . Let  $R$  be the region (including the boundary) bounded by  $L_1$ ,  $L_2$  and the  $y$ -axis.

- (a) It is given that  $R$  represents the solution of a system of inequalities. Find the system of inequalities. (3 marks)
- (b) Peter claims the value of  $-5x + 8y$ , where  $(x, y)$  is a point lying in  $R$ , must be less than 43. Do you agree? Explain your answer. (3 marks)

[22-23]

11. [S.4 22-23 Mid-Year,#4]

The coordinates of the points  $P$  and  $Q$  are  $(5, 3)$  and  $(-3, 7)$  respectively.  $P$  is rotated clockwise about  $O$  through  $90^\circ$  to  $P'$ , where  $O$  is the origin.  $Q'$  is the reflection image of  $Q$  with respect to the  $x$ -axis.

- (a) Write down the coordinates of  $P'$  and  $Q'$ .  
(b) Find the slope of  $P'Q'$ .

(4 marks)

12. [S.4 22-23 Mid-Year,#8]

In **Figure 1**, the straight line  $L_1$  passes through  $A(2, 7)$  and has the slope  $-2$ .

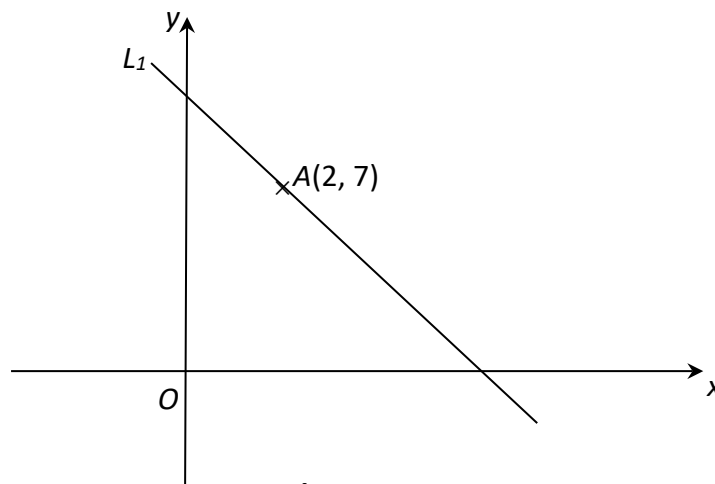


Figure 1

- (a) Find the equation of  $L_1$ . (2 marks)  
(b) If the straight line  $L_2 : kx - 3y + 1 = 0$  is parallel to  $L_1$ , find the value of  $k$ . (2 marks)  
(c)  $L_3$  is a straight line having the same  $y$ -intercept as  $L_2$  and passes through  $(-1, -3)$ . Find the equation of  $L_3$ . (2 marks)

**13. [S.4 22-23 Mid-Year,#12]**

It is given that the equation of  $L_1$  is  $2x + 5y - 2a = 0$ , where  $a$  is a positive constant.  $L_1$  cuts the  $x$ -axis and  $y$ -axis at  $A$  and  $B$  respectively.  $M$  is the mid-point of  $A$  and  $B$ .

- (a) Write down the coordinates of  $M$  in terms of  $a$ .

**(1 mark)**

- (b)  $L_2$  is the perpendicular bisector of  $AB$  and  $L_2$  cuts the  $y$ -axis at  $C$ . If  $BC = 58$ , find  $a$ .

**(3 marks)**

**14. [S.4 22-23 Final,#7]**

$L_1$  is a straight line with slope 2 and the  $y$ -intercept is  $-6$ .

- (a) Write down the equation of  $L_1$ .

- (b)  $L_2$  is another straight line that is perpendicular to  $L_1$ . If  $L_1$  and  $L_2$  have the same  $x$ -intercept, find the equation of  $L_2$ .

**(4 marks)**

**15. [S.4 22-23 Final,#15]**

It is given that  $y$  is a linear function of  $\log x$ . The slope and the intercept on the horizontal axis of the graph are 2 and  $-3$  respectively. Express the relation between  $x$  and  $y$  in the form  $x^k = 10^{y+A}$ , where  $k$  and  $A$  are constants.

**(3 marks)**

**16. [S.6 22-23 Timed Practice 7,#2]**

The coordinates of the point  $A$  are  $(2, -4)$ .  $A$  is rotated anti-clockwise about the origin  $O$  through  $90^\circ$  to  $B$ .  $C$  is the reflection image of  $A$  with respect to the  $x$ -axis.

- (a) Write down the coordinates of  $B$  and  $C$ .

- (b) Determine whether  $BC$  is perpendicular to  $AB$ .

**(4 marks)**

[23-24]

17. [S.4 23-24 Mid-Year,#7]

The slope and the  $y$ -intercept of the straight line  $L_1$  are 2 and 6 respectively.

- (a) Write down the equation of  $L_1$ .
- (b)  $L_2$  is another straight line with the same  $x$ -intercept as  $L_1$  and passes through  $(4,5)$ . Find the equation of  $L_2$ . (3 marks)

18. [S.4 23-24 Mid-Year,#8]

The straight line  $L_1: kx - 3y + 6 = 0$ , where  $k$  is a real constant, passing through  $(-6, -2)$  is perpendicular to another straight line  $L_2$ .

- (a) Find the value of  $k$ .
- (b) If  $(-1, 10)$  lies on  $L_2$ , find the equation of  $L_2$ . (5 marks)

19. [S.4 23-24 Mid-Year,#14]

The straight line  $L_1: 3x - 4y + 24k = 0$  cuts the  $x$ -axis and the  $y$ -axis at points  $A$  and  $B$  respectively, where  $k$  is a non-zero real constant. The straight line  $L_2: 3x + 2y - 30k = 0$  cuts the  $x$ -axis at  $C$  and intersects  $L_1$  at  $D$ .

- (a) Find the coordinates of  $D$  in terms of  $k$ . (2 marks)
- (b) A student claims that the ratio of the area of  $\triangle BCD$  to the area of  $\triangle BCA$  is always constant. Do you agree? Explain your answer. (2 marks)

20. [S.4 23-24 Final,#9]

A straight line  $L$  cuts the  $y$ -axis at  $A (0, 5)$  and passes through the point  $(-3, 1)$ .

- (a) Find the equation of  $L$ .
- (b) Another straight line  $\ell$  cuts the  $y$ -axis at  $B (0, 16)$  and is parallel to  $L$ . If  $\ell$  cuts the  $x$ -axis at  $P$ , find the area of  $\triangle ABP$ . (5 marks)

**21. [S.4 23-24 Final,#13]**

It is given that the equations of straight lines  $L_1$  and  $L_2$  are  $3x - 2y = 0$  and  $y = x - 4$  respectively.

$L$  is a straight line which cuts  $L_1$  and  $L_2$  at  $A$  and  $B$  respectively.  $M(0, -3)$  is the mid-point of  $A$  and  $B$ . Let  $b$  be the  $x$ -coordinate of  $B$ , where  $b > 0$ .

- (a) Write down the  $y$ -coordinate of  $B$  in terms of  $b$ . **(1 mark)**
- (b) Find the value of  $b$ . **(3 marks)**
- (c) Find the inclination of  $L$ . **(2 marks)**

**22. [S.4 23-24 Final,#16]**

It is given that  $\log_a y$  is a linear function of  $x$ , where  $a > 0$ . The slope and the intercept on the vertical axis of the graph of the linear function are  $-2$  and  $3$  respectively. If  $y = 64k^x$ , where  $k$  is a constant, find the value of  $k$ . **(3 marks)**

**23. [S.5 23-24 Mid-year,#13]**

The coordinates of points  $A$  and  $B$  are  $(-10, 7)$  and  $(-2, 1)$  respectively.  $L$  is the perpendicular bisector of  $AB$ .

- (a) Find the equation of  $L$ . **(3 marks)**
- (b) If  $L$  cuts the  $x$ -axis and the  $y$ -axis at points  $P$  and  $Q$  respectively. Find the ratio of the area of  $\triangle ABP$  to the area of  $\triangle ABQ$ . **(2 marks)**

**24. [S.6 23-24 Timed Practice 5,#3]**

The coordinates of the points  $A$  and  $B$  are  $(15, -8)$  and  $(-12, 9)$  respectively.  $A$  is rotated clockwise about the origin  $O$  through  $270^\circ$  to  $A'$ , where  $O$  is the origin.  $B'$  is the reflection image of  $B$  with respect to the  $x$ -axis.

- (a) Write down the coordinates of  $A'$  and  $B'$ .
- (b) Are  $O$ ,  $A'$  and  $B'$  collinear? Explain your answer.

**(4 marks)**