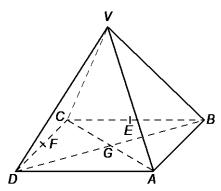
F.6 Mathematics

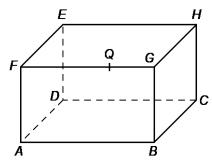
MC Exercise

6-3 Applications of Trigonometry in 3D Problems

1. In the figure, *VABCD* is a right pyramid with a square base. *E* and *F* are the mid-points of *BC* and *CD* respectively. *AC* and *BD* intersect at *G*. Which of the following is the angle between *VC* and plane *ABCD*?

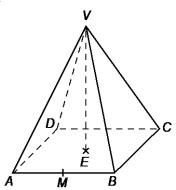


- A. $\angle BCD$
- B. $\angle VCE$
- C. ∠VCF
- D. $\angle VCG$
- 2. In the figure, ABCDEFGH is a cuboid. Q is a point lying on FG. The angle between planes ADQ and BCQ is



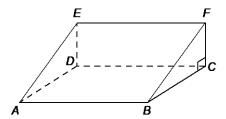
- A. $\angle AQB$.
- B. $\angle DQC$.
- C. ∠*EQH*.
- D. $\angle AQC$.

3. In the figure, *VABCD* is a right rectangular pyramid with *VE* as its height. *M* is the mid-point of *AB*.



Which of the following is **NOT** correct?

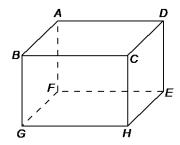
- A. $\angle AEV = 90^{\circ}$
- B. The projection of V on plane ABCD is E.
- C. The projection of VM on plane ABCD is EM.
- D. The angle between planes VAB and ABCD is $\angle MVE$.
- **4.** The figure shows a right triangular prism *ABCDEF*.



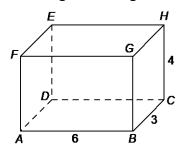
Which of the following must be correct?

- I. $\tan \angle FBC = \frac{CB}{CF}$
- II. The projection of *BE* on plane *ABCD* is *DE*.
- III. $\angle EAD$ is an angle between planes ABFE and ABCD.
- A. I only
- B. III only
- C. I and II only
- D. II and III only

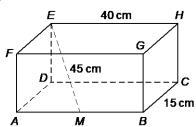
5. In the figure, ABCDEFGH is a cuboid. If AB < BC, which of the following makes the least angle with plane EFGH?



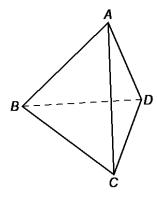
- A. GA
- B. *GB*
- C. GC
- D. GD
- 6. In the figure, ABCDEFGH is a cuboid, where AB=6, BC=3 and CH=4. Find the angle between AH and plane BCHG correct to 3 significant figures.



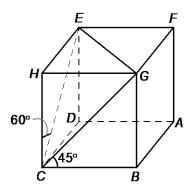
- A. 30.8°
- B. 39.8°
- C. 50.2°
- D. 63.4°
- 7. In the figure, ABCDEFGH is a cuboid. M is the mid-point of AB. It is given that $BC=15 \, \text{cm}$, $EH=40 \, \text{cm}$ and $EM=45 \, \text{cm}$. Find the angle between EM and plane ABCD correct to the nearest degree.



- A. 18°
- B. 34°
- C. 56°
- D. 63°
- **8.** In the figure, ABCD is a regular tetrahedron. Find the angle between AB and plane ADC.

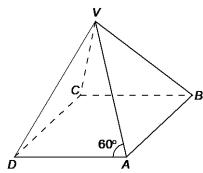


- A. 54.7° (corr. to 3 sig. fig.)
- B. 60°
- C. 62.6° (corr. to 3 sig. fig.)
- D. 70.5° (corr. to 3 sig. fig.)
- 9. In the figure, ABCDEFGH is a cuboid. Find $\angle CEG$ correct to the nearest degree.

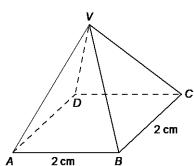


- A. 41°
- B. 52°
- C. 69°
- D. 76°

10. In the figure, VABCD is a right square pyramid, where $\angle VAD = 60^{\circ}$. Find the angle between VD and plane ABCD.

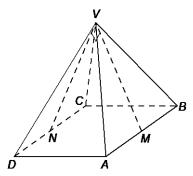


- A. 30°
- B. 45°
- C. 60°
- D. 90°
- 11. In the figure, VABCD is a right pyramid of height 2 cm, where its base ABCD is a square with sides of 2 cm each. If the angle between planes VAB and VCD is θ , find $\tan \theta$.

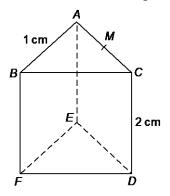


- A. 1
- B. $\frac{4}{3}$
- C. $2\sqrt{3}$
- D. 4

12. In the figure, VABCD is a right pyramid with a square base. M and N are the mid-points of AB and DC respectively. If $\angle MVN = 90^{\circ}$, find $\angle VMD$ correct to 3 significant figures.



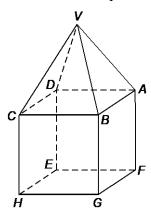
- A. 35.3°
- B. 39.2°
- C. 50.8°
- D. 54.7°
- 13. In the figure, ABCDEF is a right triangular prism, where $\triangle ABC$ is an equilateral triangle of side 1 cm. The height of the prism is 2 cm. M is the mid-point of AC.



Which of the following angles is the largest?

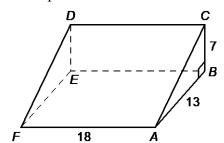
- A. ∠*FAD*
- B. $\angle FED$
- C. ∠FAB
- D. $\angle FMB$

14. In the figure, a solid is formed by a cube *ABCDEFGH* and a right square pyramid *VABCD* with all sides equal.



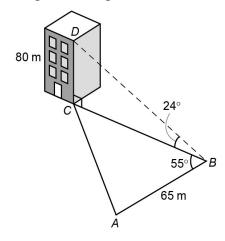
Which of the following must be right angle(s)?

- I. ∠EFB
- II. ∠*VBE*
- III. ∠BFD
- A. I only
- B. III only
- C. I and II only
- D. II and III only
- 15. In the figure, ABEF is a rectangular horizontal plane and ACDF is a rectangular inclined plane, where C and D are vertically above B and E respectively. It is given that AF=18, AB=13 and BC=7. Find the inclination of CF correct to 1 decimal place.

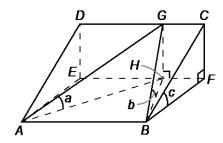


- A. 16.7°
- B. 17.5°
- C. 19.4°
- D. 28.3°

16. In the figure, ABC is a horizontal plane and CD is a building of height 80 m standing vertically on C. The angle of elevation of D from B is 24° , $\angle ABC = 55^{\circ}$ and AB = 65 m. Find the length of AC correct to 3 significant figures.

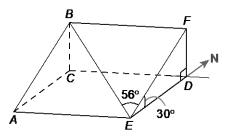


- A. 132 m
- B. 152 m
- C. 172 m
- D. 179 m
- 17. In the figure, ABFE is a rectangular horizontal plane and ABCD is a rectangular inclined plane, where D and C are vertically above E and F respectively. G and H are points lying on DC and EF respectively such that $GH \perp EF$. It is given that EH > HF. If $\angle GAH = a$, $\angle GBH = b$ and $\angle CBF = c$, which of the following must be true?

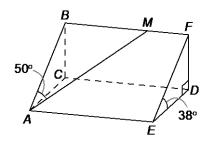


- A. a > b > c
- B. b > a > c
- C. b > c > a
- D. c > b > a

18. In the figure, *ACDE* is a rectangular horizontal plane, *ABFE* is a rectangular inclined plane where its inclination is 30°. *E* is due south of *D*. *BE* makes an angle of 56° with the line of greatest slope *EF*. Find the compass bearing of *B* from *E* correct to 3 significant figures.

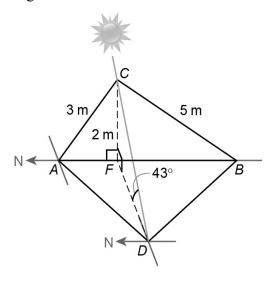


- A. N30.3°W
- B. N37.9°W
- C. N52.1°W
- D. N59.7°W
- 19. In the figure, ACDE is a rectangular horizontal plane, ABFE is a rectangular inclined plane where its inclination is 38° . If M is a point on BF such that BM: MF = 2:1 and $\angle BAM = 50^{\circ}$, find the inclination of AM correct to 3 significant figures.

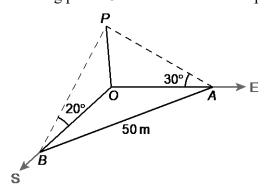


- A. 23.3°
- B. 31.7°
- C. 66.7°
- D. 73.3°
- 20. In the figure, ABC is a wall standing vertically on the horizontal ground, where A is due north of B, AC = 3 m and BC = 5 m. F is the foot of perpendicular from C to AB, where CF = 2 m. When the sun shines from the east with an angle of elevation of 43° , the shadow of the wall on the horizontal ground is ΔABD . Find the

area of shadow ABD correct to 3 significant figures.

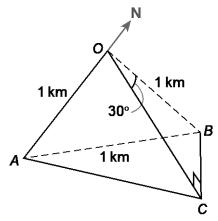


- A. $7.31 \,\mathrm{m}^2$
- B. $7.50 \,\mathrm{m}^2$
- C. 8.04 m^2
- D. $8.41 \,\mathrm{m}^2$
- 21. In the figure, O, A and B are three points on the same horizontal plane, where A is due east of O and B is due south of O. PO is a flag pole which stands vertically on the horizontal plane. If $AB = 50 \,\text{m}$ and the angles of elevation of P from A and B are 30° and 20° respectively, find the height of the flag pole PO correct to 1 decimal place.



- A. 15.4 m
- B. 19.9 m
- C. 29.2 m
- D. 93.7 m

22. In the figure, O, A and C are three points on a horizontal plane, where A is due south of O. B is a point vertically above C. The angle of elevation of B from O is 30° . If OA = OB = AB = 1 km, find the compass bearing of B from O correct to 1 decimal place.



- A. N54.7°E
- B. S54.7°E
- C. N35.3°E
- D. S35.3°E

