## **F.6 Mathematics**

## **MC** Exercise

## **6-2 Geometric Sequences**

- 1. It is given that the general term of a geometric sequence is  $T_n = \left(-\frac{3}{5}\right)^{2n-1}$ . Find the common ratio of the sequence.
  - A.  $-\frac{3}{5}$
  - B.  $\frac{3}{5}$
  - C.  $-\frac{9}{25}$
  - D.  $\frac{9}{25}$
- 2. Find the general term  $T_n$  of the geometric sequence 12, -24, 48, -96, ...
  - A.  $-3(2)^n$
  - B.  $-3(2)^{n+1}$
  - C.  $3(-2)^n$
  - D.  $3(-2)^{n+1}$
- 3. Find the number of terms in the geometric sequence  $a^6$ ,  $a^9$ ,  $a^{12}$ , ...,  $a^{60}$ .
  - A. 18
  - B. 19
  - C. 20
  - D. 21
- **4.** It is given that the (n+1) th term of a geometric sequence is  $2(-3)^{2-n}$ , where n > -1. Find the first term and the common ratio of the sequence.

	First term	Common ratio
A.	-6	$-\frac{1}{3}$
B.	-6	-3
C.	18	$-\frac{1}{3}$
D.	18	-3

- 5. If the 3rd term and the 8th term of a geometric sequence are -63 and 15 309 respectively, then the common ratio of the sequence is
  - A. -7.
  - B. -3.
  - C. ±3.
  - D. ±7.
- 6. If x+1, 4x+4, 160-2x form a geometric sequence, find the value(s) of x.
  - A. 17
  - B. 8
  - C. -1
  - D. 8 or -1
- 7. If a, b, c form a geometric sequence, where a+b+c=6 and abc=-64, then a+c=
  - A. -4.
  - B. 2.
  - C. 4.
  - D. 10.

- 8. If x, y, z form a geometric sequence with the common ratio of r, then the common ratio of the geometric sequence  $3x^2$ ,  $3y^2$ ,  $3z^2$  is
  - A. 2*r*.
  - B. 3*r*.
  - C.  $r^2$ .
  - D.  $r^3$ .
- **9.** Which of the following must be true?
  - I. A sequence with the general term  $T_n = \frac{4^{n+2}}{7^{2n-1}} \text{ is a geometric sequence.}$
  - II. A sequence with the general term  $T_n = \frac{2^{n^2+1}}{3^{n^2+3}} \text{ is a geometric sequence.}$
  - III. A sequence with the general term  $T_n$ , where  $T_2 = 40$ ,  $T_4 = 10$  and  $T_6 = \frac{5}{4}$ , is a geometric sequence.
  - A. I only
  - B. I and II only
  - C. II and III only
  - D. I, II and III
- 10. Consider the geometric sequence -288, -192, -128,  $\cdots$ . If the *k*th term of the sequence is greater than -0.1, find the minimum value of *k*.
  - A. 19
  - B. 20
  - C. 21
  - D. 22

- 11. Let  $T_n$  be the general term of a geometric sequence with common ratio r, where 0 < r < 1. It is given that  $T_1 + T_2 + T_3 = 19$  and  $T_1T_2T_3 = 216$ . Find  $T_1 T_3$ .
  - A. 5
  - B.  $\sqrt{97}$
  - C. 13
  - D. Cannot be determined
- 12. Find the sum of the first 7 terms of the geometric sequence 4, 20, 100, 500, ....
  - A. 15 624
  - B. 62 500
  - C. 78 124
  - D. 390 624
- 13. Find the value of the geometric series  $2^2 + 2^4 + 2^6 + \cdots + 2^{14}$ .
  - A. 16383
  - B. 21844
  - C. 32 766
  - D. 65 532
- 14. It is given that  $a \neq b$  and  $b \neq 1$ . The value of the geometric series  $a^{100} + a^{99}b + a^{98}b^2 + \cdots + b^{100}$  is
  - A.  $\frac{a^{100}(b^{100}-1)}{b-1}$ .
  - B.  $\frac{a^{100}(b^{101}-1)}{b-1}$ .
  - C.  $\frac{b^{100}-a^{100}}{b-a}$ .
  - D.  $\frac{b^{101}-a^{101}}{b-a}$ .

- 15. If the sum of the first m terms of the geometric sequence -12, -48, -192,  $\cdots$  is smaller than  $-10^6$ , find the minimum value of m.
  - A. 7
  - B. 8
  - C. 9
  - D. 10
- 16. Find the sum of all positive terms of the geometric sequence -3, 6, -12, 24, -48, 96,  $\cdots$ , 24 576.
  - A. 8 190
  - B. 16 383
  - C. 32 766
  - D. 49 149
- 17. Find the sum of the 6th to 10th terms of the geometric sequence  $7, -21, 63, \cdots$ .
  - A. -104 608
  - B. -103 761
  - C. -34 587
  - D. 309 582
- 18. The sum of the first 3 terms of a geometric sequence is 1 008, and the sum of the following 3 terms is -126. Find the common ratio of the sequence.
  - A. -8
  - B.  $-\frac{1}{8}$
  - C. –2
  - D.  $-\frac{1}{2}$

- 19.  $9 \times 9^3 \times 9^9 \times 9^{27} \times \cdots \times 9^{3^n} =$ 
  - A.  $3^{3^n}$ .
  - B.  $3^{3^{n+1}-1}$ .
  - C.  $3^{\frac{3}{2}(3^n+1)}$ .
  - D.  $3^{n+2}$ .
- **20.** Let  $a_n$  be the *n*th term of a geometric sequence. If  $a_4 > 0$  and  $a_7 < 0$ , which of the following must be true?
  - I.  $a_1 < 0$
  - II.  $a_3 = \sqrt{a_2 a_4}$
  - III.  $a_1 + a_2 + a_3 + \dots + a_7 < 0$
  - A. I and II only
  - B. I and III only
  - C. II and III only
  - D. I, II and III
- 21. Find the value of the geometric series  $6+0.6+0.06+\cdots$ 
  - A.  $\frac{2}{3}$
  - B. 666
  - C. 667
  - D.  $6\frac{2}{3}$
- **22.** Find the value of

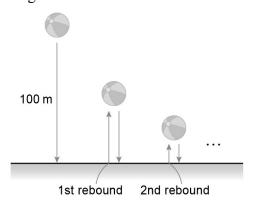
$$\frac{1}{3} - \frac{2}{3^2} + \frac{1}{3^3} - \frac{2}{3^4} + \frac{1}{3^5} - \frac{2}{3^6} + \cdots$$

- A.  $\frac{1}{8}$
- B.  $\frac{1}{5}$
- C.  $\frac{5}{8}$
- D. 1

- 23. It is given that the sum to infinity of a geometric sequence is 35 and the first term is 20. Find the common ratio of the sequence.
  - A.  $-\frac{4}{7}$
  - B.  $-\frac{3}{7}$
  - C.  $\frac{3}{7}$
  - D.  $\frac{4}{7}$
- 24. If  $1 + \sin\theta + \sin^2\theta + \dots = 2(2 + \sqrt{3})$ , where  $0^\circ < \theta < 90^\circ$ , find the value(s) of  $\cos\theta$ .
  - A.  $\frac{1}{2}$
  - B.  $\frac{\sqrt{3}}{2}$
  - C.  $\frac{1}{2}$  or  $-\frac{1}{2}$
  - D.  $\frac{\sqrt{3}}{2}$  or  $-\frac{\sqrt{3}}{2}$
- **25.** It is given that 4, k and  $k \frac{8}{9}$  are the first 3 terms of a geometric sequence. Find the sum to infinity of the sequence.
  - A.  $\frac{1}{3}$
  - B.  $\frac{4}{3}$
  - C. 6
  - D. 6 or 12
- 26. The 2nd and the 4th terms of a geometric sequence are -35 and  $-\frac{35}{16}$  respectively. Find the sum to infinity of the sequence.

- A.  $-\frac{560}{3}$
- B.  $\frac{560}{3}$
- C.  $\frac{560}{3}$  or -112
- D.  $-\frac{560}{3}$  or 112
- 27. If the sum of the first 2 terms of a geometric sequence is 35 and the sum to infinity is 63, find the first term of the sequence.
  - A. -21
  - B.  $\frac{2}{3}$  or  $-\frac{2}{3}$
  - C. 28
  - D. 21 or 105
- **28.** It is given that the sum to infinity of the geometric sequence  $T_1, T_2, T_3, \cdots$  is  $\frac{2}{3}T_1$ . Find  $T_2 + T_4 + T_6 + \cdots$ .
  - A.  $-\frac{2}{3}T_1$
  - B.  $-\frac{1}{3}T_1$
  - C.  $\frac{1}{3}T_1$
  - D.  $\frac{4}{3}T_1$
- 29. Consider the geometric sequence  $x^2$ ,  $3x^3$ ,  $9x^4$ , ... If the sum to infinity of the geometric sequence exists, which of the following is a possible value of x?
  - A. 0
  - B.  $\frac{1}{2}$
  - C.  $\frac{1}{3}$
  - D.  $\frac{1}{4}$

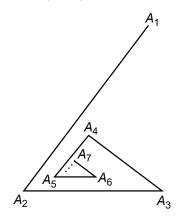
- **30.** Air is leaking out from a balloon. In the first minute, 30 cm<sup>3</sup> of air leaks out from the balloon. After that, the volume of air leaked in each minute is 70% of that in the preceding minute. What is the total volume of air leaked in the first 5 minutes?
  - A.  $5.0421 \text{ cm}^3$
  - B. 42.753 cm<sup>3</sup>
  - C.  $75.99 \text{ cm}^3$
  - D. 83.193 cm<sup>3</sup>
- **31.** A ball is dropped from a spot of 100 m above the ground. After each rebound, the ball only rises to half of its preceding height.



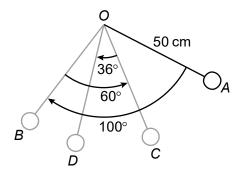
How many rebounds will the ball make when it travels a distance of 290 m?

- A. 4
- B. 5
- C. 6
- D. 7
- 32. Raymond's monthly salary is \$10 000 this year and it increases by 10% each year. If Raymond saves 20% of his monthly salary every month, at least how many years later will his total savings exceed \$200 000?
  - A. 6 years
  - B. 7 years
  - C. 8 years
  - D. 9 years

33. The figure is formed by an infinite number of line segments  $A_1A_2$ ,  $A_2A_3$ ,  $A_3A_4$ , ..., where  $A_2A_3 = \frac{2}{3}A_1A_2$ ,  $A_3A_4 = \frac{2}{3}A_2A_3$ , .... If  $A_1A_2 = 90 \text{ cm}$ , find  $A_1A_2 + A_2A_3 + A_3A_4 + \cdots$ .



- A. 54 cm
- B. 270 cm
- C. 405 cm
- D. 540 cm
- 34. The figure shows a pendulum with the length of 50 cm. It is released from A and it keeps swinging until it comes to rest. The angles swung  $\angle AOB$ ,  $\angle BOC$ ,  $\angle COD$ ,  $\cdots$  form a geometric sequence. Find the total distance travelled by the end of the pendulum  $\widehat{AB} + \widehat{BC} + \widehat{CD} + \cdots$ .



- A.  $\frac{125\pi}{3}$  cm
- B.  $\frac{625\pi}{3}$  cm
- C.  $\frac{625\pi}{9}$  cm
- D.  $\frac{625\pi}{18}$  cm

