

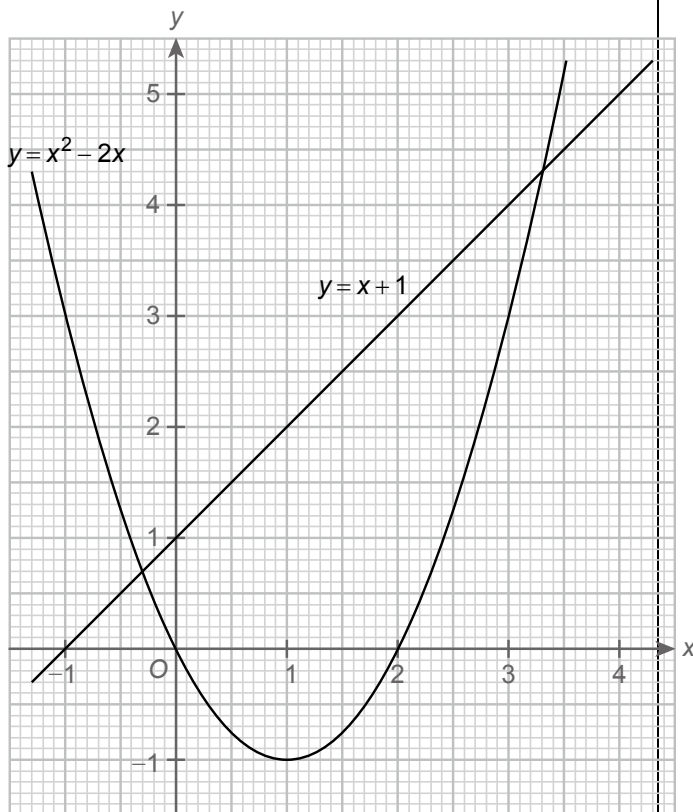
F.4 Mathematics

MC Exercise

4B9 More About Equations

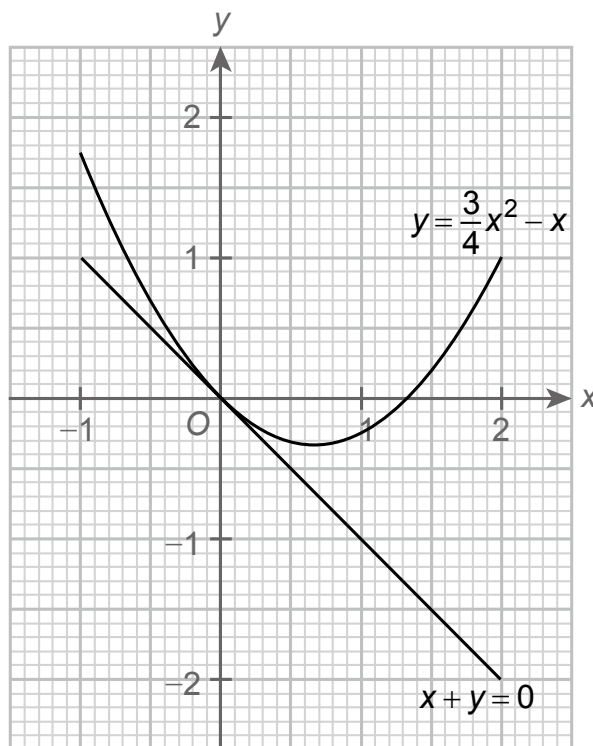
1. If $\begin{cases} y = x^2 + 4x \\ y = -6x - 25 \end{cases}$, then $x =$
- A. -5 .
B. 5 .
C. 0 or -5 .
D. 0 or 5 .
2. If $\begin{cases} x^2 + 2x + 3y = 11 \\ 3x + 2y = 8 \end{cases}$, then $x =$
- A. 2 .
B. -2 .
C. $\frac{1}{2}$ or 2 .
D. $-\frac{1}{2}$ or -2 .
3. If $x + 2y = 2y + x(x + 2) = 4$, then $x =$
- A. 0 .
B. -1 or 0 .
C. 0 or 2 .
D. -1 or 2 .
4. How many sets of real solutions do the simultaneous equations $\begin{cases} y = x^2 - 2x + 10 \\ y = -6x - 26 \end{cases}$ have?
- A. 0
B. 1
C. 2
D. 4
5. Let a and b be constants. If $\begin{cases} x = 2 \\ y = 1 \end{cases}$ is a solution of the simultaneous equations $\begin{cases} y = 2x^2 + ax + b \\ y = 3x + a \end{cases}$, then $b =$
- A. -5 .
B. -1 .
C. 1 .
D. 3 .
6. Let k be a constant. If the simultaneous equations $\begin{cases} y = x^2 - x + 3 \\ y = kx - 1 \end{cases}$ have only one set of real solution, find the values of k .
- A. 1 or -3
B. -1 or 3
C. -3 or 5
D. 3 or -5
7. Let k be a constant. If the simultaneous equations $\begin{cases} x^2 + y^2 = k \\ y = 2x + 5 \end{cases}$ have real solutions, find the range of values of k .
- A. $k > 5$
B. $k \geq 5$
C. $k < 5$
D. $k \leq 5$

8. The figure shows the graphs of $y = x^2 - 2x$ and $y = x + 1$. Solve the simultaneous equations $\begin{cases} y = x^2 - 2x \\ y = x + 1 \end{cases}$ graphically.



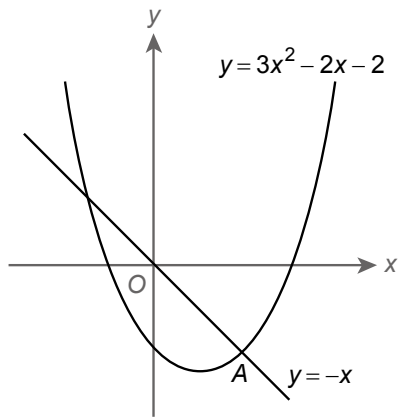
- A. $x = 0.0, y = 0.0$ and $x = 2.0, y = 0.0$ (corr. to 1 d.p.)
- B. $x = -0.3, y = 0.7$ and $x = 3.3, y = 4.3$ (corr. to 1 d.p.)
- C. $x = -1.0, y = 0.0$ and $x = 3.3, y = 4.3$ (corr. to 1 d.p.)
- D. $x = 0.0, y = 0.0$ and $x = 0.0, y = 1.0$ (corr. to 1 d.p.)

9. The figure shows the graphs of $y = \frac{3}{4}x^2 - x$ and $x + y = 0$, where $-1 \leq x \leq 2$. Solve the simultaneous equations $\begin{cases} y = \frac{3}{4}x^2 - x \\ x + y = 0 \end{cases}$ graphically.



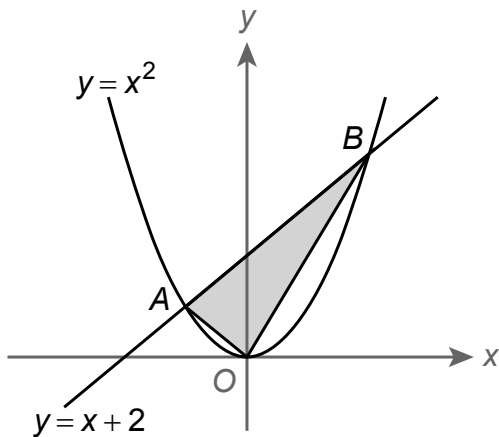
- A. $x = 0.0, y = 0.0$ (corr. to 1 d.p.)
- B. $x = 0.0, y = 0.0$ and $x = 1.3, y = 0.0$ (corr. to 1 d.p.)
- C. $x = 1.0, y = -0.3$ and $x = 1.0, y = -1.0$ (corr. to 1 d.p.)
- D. There are no real solutions.

10. In the figure, find the coordinates of A .



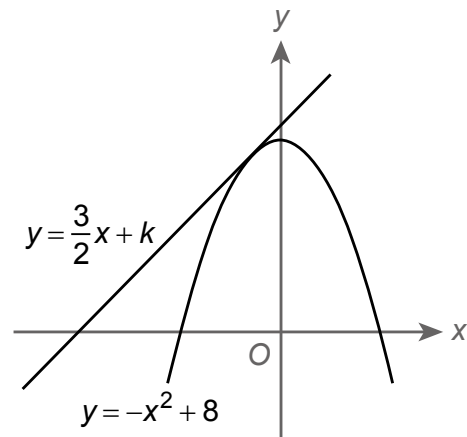
- A. $\left(-\frac{2}{3}, \frac{2}{3}\right)$
 B. $\left(\frac{1}{3}, -\frac{1}{3}\right)$
 C. $(1, -1)$
 D. $\left(\frac{3}{2}, -\frac{3}{2}\right)$

11. In the figure, the graphs of $y = x^2$ and $y = x + 2$ intersect at A and B . Find the area of $\triangle OAB$.



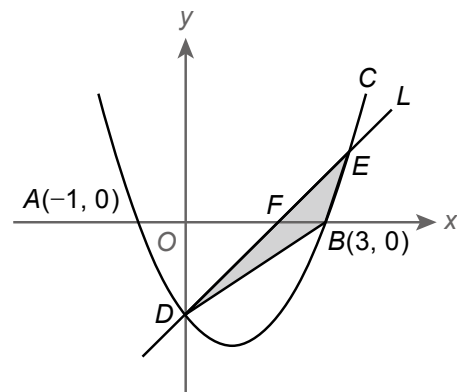
- A. 3 square units
 B. 3.75 square units
 C. 6 square units
 D. 7.5 square units

12. In the figure, the curve $y = -x^2 + 8$ and the straight line $y = \frac{3}{2}x + k$ touch at only one point. Find the value of k .



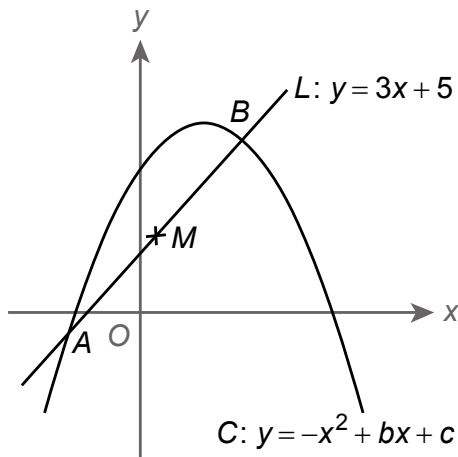
- A. $\frac{9}{4}$
 B. 8
 C. $\frac{67}{8}$
 D. $\frac{137}{16}$

13. In the figure, the curve $C: y = x^2 - 2x - 3$ cuts the x -axis at $A(-1, 0)$ and $B(3, 0)$. The straight line $L: y = \frac{3}{2}x - 3$ cuts the x -axis at F , and it cuts C at D and E where D lies on the y -axis. Find the area of $\triangle DEB$.



- A. $\frac{9}{8}$ square units
 B. $\frac{3}{2}$ square units
 C. $\frac{21}{8}$ square units
 D. $\frac{21}{4}$ square units

14. In the figure, a straight line $L: y = 3x + 5$ and a curve $C: y = -x^2 + bx + c$ intersect at A and B . M is the mid-point of AB . Find the coordinates of M .



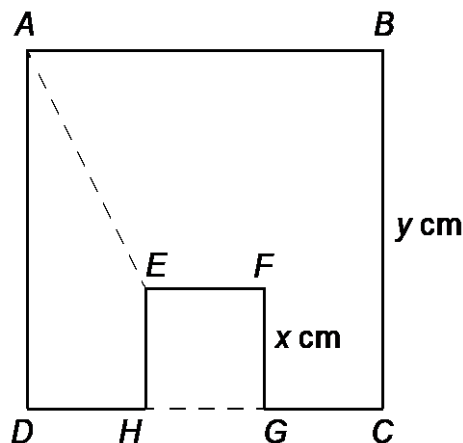
- A. $\left(-\frac{3}{2}, \frac{1}{2}\right)$
 B. $\left(-\frac{b}{2}, \frac{10-3b}{2}\right)$
 C. $\left(\frac{3-b}{2}, \frac{19-3b}{2}\right)$
 D. $\left(\frac{b-3}{2}, \frac{3b+1}{2}\right)$
15. Solve $x - \sqrt{x} = \sqrt{x} - 1$.
 A. $x = 0$
 B. $x = 1$
 C. $x = \pm 1$
 D. No real solutions
16. If $\frac{1}{2x+3} + x = \frac{3}{4}$, then $x =$
 A. $\frac{1}{2}$.
 B. $\frac{9}{2}$.
 C. $\frac{1}{2}$ or $-\frac{5}{4}$.
 D. $-\frac{1}{2}$ or $\frac{5}{4}$.

17. If $\sqrt{x} + 1 - \sqrt{\sqrt{x} + 1} = 0$, then $x =$
 A. 0.
 B. 1.
 C. 0 or 1.
 D. 0 or ± 1 .
18. How many distinct real roots does the equation $x^6 - 5x^4 + 4x^2 = 0$ have?
 A. 3
 B. 4
 C. 5
 D. 6
19. If $36^x + 6^{x+1} - 72 = 0$, then $x =$
 A. 0.
 B. 1.
 C. -1 or 1.
 D. 6 or -12.
20. If $\log_3(x-1) = 1 - \log_3(3x-11)$, then $x =$
 A. 4.
 B. $\frac{13}{4}$.
 C. $\frac{2}{3}$ or 4.
 D. $\frac{2}{3}$ or $\frac{13}{4}$.
21. If $(\log x^2)^2 = 2 \log x^2$, then $x =$
 A. 0 or 2.
 B. 0, 1 or 10.
 C. 1 or 10.
 D. ± 1 or ± 10 .
22. If $x^4 + \log y^3 = x^2 + \log \frac{1}{y} = 1$, then $x =$
 A. 0.
 B. 1.
 C. ± 1 .
 D. ± 1 or ± 2 .

23. How many distinct real solutions does the equation $2^{2x} + 5(2^x) - 24 = 0$ have?

A. 0
B. 1
C. 2
D. 4

24. In the figure, $ABCD$ and $EFGH$ are two squares of sides y cm and x cm respectively. It is given that $DH = HE$ and the perimeter of $ABCGFEHD$ is 22 cm.



If the distance between A and E is $\sqrt{17}$ cm, which of the following simultaneous equations can be used to find the values of x and y ?

- A.
$$\begin{cases} y + x = \frac{11}{2} \\ (y - x)^2 + x^2 = 17 \end{cases}$$

B.
$$\begin{cases} y + x = \frac{11}{2} \\ (y - 2x)^2 + x^2 = 17 \end{cases}$$

C.
$$\begin{cases} 2y + x = 11 \\ (y - x)^2 + x^2 = 17 \end{cases}$$

D.
$$\begin{cases} 2y + x = 11 \\ (y - 2x)^2 + x^2 = 17 \end{cases}$$

25. Judy spent \$720 on x cups of puddings for Christmas party. If the price of each cup of pudding reduces by \$2, she can buy $(x + 4)$ cups of puddings with the same amount of money. Which of the following equations can be used to find the value of x ?

- A.
$$\frac{720}{x} + 2 = \frac{720}{x + 4}$$

B.
$$\frac{720}{x} - 2 = \frac{720}{x + 4}$$

C.
$$\frac{720}{x} = \frac{720 - 2x}{x + 4}$$

D.
$$\frac{720}{x} = \frac{720 - 2x}{x - 4}$$

26. In a journey of 300 km long, if the driving speed of a car increases by 10 km/h, the travelling time will reduce by 1 hour. Which of the following equations can be used to find the original driving speed x km/h of the car?

- A.
$$\frac{300}{x} - \frac{300}{x + 10} = 1$$

B.
$$\frac{300}{x - 10} - \frac{300}{x} = 1$$

C.
$$\frac{300}{x} - \frac{300}{x + 10} = 60$$

D.
$$\frac{300}{x - 10} - \frac{300}{x} = 60$$

27. Kent bought n pears for \$875 but 12 of them were rotten. He sold the rest of the pears at a price of \$1.5 more than the cost each. Finally, he made a profit of 36%. Which of the following equations can be used to find the value of n ?

- A. $1.5(n - 12) = 875 \times 36\%$
B. $1.5n - \frac{875}{n} \times 12 = 875 \times 36\%$
C. $\left(\frac{875}{n} + 1.5\right)(n - 12) = 875(1 + 36\%)$
D. $\left(\frac{875}{n - 12} + 1.5\right)(n - 12) = 875(1 + 36\%)$

28. It is given that the sum of the reciprocals of two consecutive odd numbers is $\frac{16}{63}$. If x is the smaller number, then $x =$
- A. 5.
B. 7.
C. 9.
D. 11.
29. $(i^{51})^{86} =$
- A. 1.
B. -1 .
C. i .
D. $-i$.
30. $(8 - 11i)^2 - (73 + i) =$
- A. $112 - i$.
B. $-130 - i$.
C. $112 - 177i$.
D. $-130 - 177i$.
31. If k is a real number, then $\frac{3 + ki}{i} - i =$
- A. $k + 2i$.
B. $k - 4i$.
C. $(k - 1) - 3i$.
D. $(k - 1) + 3i$.
32. The real part of $i - i^2 + i^3 - i^4 + i^5$ is
- A. -1 .
B. 0 .
C. 1 .
D. 3 .
33. The imaginary part of $(3 + 2i)(1 - 2i) - 3i$ is
- A. 3 .
B. -3 .
C. 7 .
D. -7 .
34. It is given that $z = i(3 - xi) - 4$, where x is a real number. If z is a purely imaginary number, then $x =$
- A. -3 .
B. 3 .
C. -4 .
D. 4 .
35. If β is a real number, then $\frac{\beta^2 + 1}{(\beta + i)^2} =$
- A. 1 .
B. $\frac{\beta^2 + 1}{\beta^2 - 1}$.
C. $\frac{\beta^2 - 1}{\beta^2 + 1}$.
D. $\frac{\beta^2 - 1}{\beta^2 + 1} - \frac{2\beta}{\beta^2 + 1}i$.
36. It is given that $(x + 2i)(y + i) = 1 + 5i$, where x and y are real numbers. Find the value(s) of y .
- A. $-\frac{2}{3}$
B. 1
C. $\frac{3}{2}$ or 1
D. $-\frac{3}{2}$ or -1

