## 2021-2022 S5 1st TERM UT-MATH-CP 2



# MATHEMATICS Compulsory Part 

## PAPER 2

$8^{\text {th }}$ November, 2021<br>9:15 am - 9:45 am (30 minutes)

## INSTRUCTIONS

1. Read carefully the instructions on the Answer Sheet. After the announcement of the start of the examination, you should insert the information required in the spaces provided.
2. When told to open this book, you should check that all the questions are there. Look for the words 'END OF PAPER' after the last question.
3. All questions carry equal marks.
4. ANSWER ALL QUESTIONS. You should use an HB pencil to mark all your answers on the Answer Sheet, so that wrong marks can be completely erased with a clean rubber. You must mark the answers clearly; otherwise you will lose marks if the answers cannot be captured.
5. You should mark only ONE answer for each question. If you mark more than one answer, you will receive NO MARKS for that question.
6. No marks will be deducted for wrong answers.

There are 11 questions in Section $\mathbf{A}$ and 7 questions in Section B.
The diagrams in this paper are not necessarily drawn to scale.
Choose the best answer for each question.

## Section A

1. $\frac{4 x^{2}}{\left(2 x^{-3}\right)^{4}}=$
A. $\frac{x^{14}}{4}$.
B. $2 x^{14}$.
C. $\frac{2}{x^{10}}$.
D. $\frac{x^{10}}{4}$.
2. In the figure, a solid consists of a right cylinder and a hemisphere with a common base. The radius of the hemisphere is 6 cm and volume of the solid is $432 \pi \mathrm{~cm}^{3}$. Find the total surface area of the solid.
A. $96 \pi \mathrm{~cm}^{2}$
B. $168 \pi \mathrm{~cm}^{2}$
C. $204 \pi \mathrm{~cm}^{2}$
D. $240 \pi \mathrm{~cm}^{2}$

3. If $p<q<0$, which of the following must be true?
A. $p+q>0$
B. $p^{2}<q^{2}$
C. $\frac{1}{p}<\frac{1}{q}$
D. $\frac{p}{q}>1$
4. Solve $-4 x-3>5$ or $3 x+1 \leq x+3$.
A. $x<-2$
B. $x \leq 1$
C. $-2<x \leq 1$
D. All real numbers
5. It is given that $y$ varies directly as $x^{2}$. When $x=3, y=54$. Find the value(s) of $x$ when $y=150$.
A. 5
B. 6
C. 25
D. 5 or -5
6. If $p$ varies directly as the square root of $q$ and inversely as $r$, which of the following must be a constant?
A. $\frac{p^{2} r^{2}}{q}$
B. $\frac{p r}{q^{2}}$
C. $p \sqrt{q} r$
D. $\frac{p \sqrt{q}}{r}$
7. It is given that $f(x)$ is partly constant and partly varies inversely as the square of $x$. If $f(1)=11$ and $f(4)=-4$, then $f(-2)=$
A. -9 .
B. -1 .
C. 3 .
D. 16 .
8. It is given that $y$ varies as $x$ and $z$. If $x$ is increased by $20 \%$ and $z$ is decreased by $30 \%$, then
A. $y$ is increased by $4 \%$.
B. $y$ is decreased by $6 \%$.
C. $y$ is decreased by $10 \%$.
D. $y$ is decreased by $16 \%$.
9. Given a straight line $4 x-3 y-24=0$. Which of the following must be true?
I. The slope of the straight line is $\frac{4}{3}$.
II. $y$-intercept is positive.
III. $x$-intercept is 6 .
A. I only
B. I and III only
C. II and III only
D. I, II and III
10. Find the median and the range of the set of data $\{41,37,33,30,44,43,55,59\}$.

|  | Median | Range |
| :--- | :---: | :---: |
| A. | 42 | 18 |
| B. | 42 | 29 |
| C. | 42.75 | 18 |
| D. | 42.75 | 29 |

11. The stem-and-leaf diagram below shows the distribution of the heights (in cm ) of the students of class 5B. Find the mode, median and range of the distribution.

| Stem (tens) | Leaf (units) |
| ---: | :--- |
| 15 | 0599 |
| 16 | 000123346677789 |
| 17 | 1122255777799 |
| 18 | 004 |


|  | $\frac{\text { Mode }}{}$ |  | Median |  |
| :--- | :---: | :--- | :--- | :--- |
| A. Range |  |  |  |  |
| A. | 7 cm | 168 cm |  | 30 cm |
| B. | 7 cm | 169 cm | 34 cm |  |
| C. | 177 cm | 168 cm | 34 cm |  |
| D. | 177 cm | 169 cm | 30 cm |  |

## Section B

12. The solutions of $x^{2}-10 x+21>0$ are
A. $x<3$.
B. $x<7$.
C. $3<x<7$.
D. $x<3$ or $x>7$.
13. Which of the following points lies in the feasible region of $\left\{\begin{array}{l}y \leq 2 x-1 \\ x+y-4>0 \\ 5 x-2 y<7\end{array}\right.$ ?
A. $(0,3)$
B. $(2,0)$
C. $(2,3)$
D. $(4,6)$
14. Which of the following systems of inequalities has its solutions represented by the shaded region in the figure?

A. $\left\{\begin{array}{l}3 x+5 y \leq 15 \\ x<2\end{array}\right.$
B. $\left\{\begin{array}{l}3 x+5 y \leq 15 \\ x>2\end{array}\right.$
C. $\left\{\begin{array}{l}3 x+5 y \geq 15 \\ x<2\end{array}\right.$
D. $\left\{\begin{array}{l}3 x+5 y \geq 15 \\ x>2\end{array}\right.$
15. Which of the region in the figure may represent the solution of $\left\{\begin{array}{c}3 x+y>6 \\ y \\ x+y \leq 4\end{array}\right.$ ?

A. Region I
B. Region II
C. Region III
D. Region IV
16. A chef has 10 kg meat, 9 kg seafood and 15 kg vegetables. He has to make two kinds of dishes $A$ and $B$. The following table shows the ingredients required to make these two dishes.

| Dish | Meat $(\mathrm{g})$ | Seafood $(\mathrm{g})$ | Vegetables $(\mathrm{g})$ |
| :---: | :---: | :---: | :---: |
| $A$ | 200 | 90 | 50 |
| $B$ | 100 | 180 | 250 |

The profits of each dish $A$ and dish $B$ are $\$ 30$ and $\$ 40$ respectively. Suppose that the chef makes $x$ dishes $A$ and $y$ dishes $B$. Which of the following is a constraint about $x$ and $y$ ?
A. $30 x+40 y \leq 0$
B. $200 x+100 y \leq 10$
C. $10 x+50 y \leq 3$
D. $x+2 y \leq 100$
17. The graph in the figure shows the linear relation between $x$ and $\log _{5} y$. If $y=a b^{x}$, then $b=$

A. $\frac{1}{125}$.
B. $\frac{1}{1000}$.
C. $\frac{1}{\sqrt[5]{125}}$.
D. $\frac{1}{\sqrt[5]{1000}}$.
18. It is given that $x>0$ and $x \neq 1$. Find the value of $\frac{5 \log \sqrt{x}-\log \sqrt[3]{x}}{\log x^{2}+3 \log \frac{1}{x}}$.
A. $-\frac{13}{6}$
B. -1
C. $\frac{1}{5}$
D. $\frac{13}{30}$

