19-20 F. 4 2nd TERM EXAM MATH CP PAPER 1

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2019-2020
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Form 4 Second Term Examination

## MATHEMATICS Compulsory Part

## PAPER 1

## Question-Answer Book

$24^{\text {th }}$ June, 2020
8:15 am - 9:45 am (1 hour 30 minutes)
This paper must be answered in English

## INSTRUCTIONS

1. Write your name, class and class number in the spaces provided on this cover.
2. This paper consists of THREE sections, $\mathrm{A}(1)$, $\mathrm{A}(2)$ and B .
3. Attempt ALL questions in this paper. Write your answers in the spaces provided in this Question - Answer Book. Do not write in the margins. Answers written in the margins will not be marked.
4. Unless otherwise specified, all working must be clearly shown.
5. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
6. The diagrams in this paper are not necessarily drawn to scale.

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| Sections | Marks |
| :---: | ---: |
| $\mathrm{A}(1-4)$ | $/ 14$ |
| $\mathrm{~A}(5-10)$ | $/ 28$ |
| A Total | $/ \mathbf{4 2}$ |
| B Total | $/ \mathbf{7 0}$ |
| TOTAL |  |

## Section A(1) (18 marks)

1. Make $a$ the subject of the formula $2 c(5 a+3 b)=7 a$.
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2. Simplify $\frac{b^{3}}{\left(2 a^{6} b^{-3}\right)^{-2}}$ and express your answer with positive indices.
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Answers written in the margins will not be marked.
3. Factorize
(a) $8 a-20 b$,
(b) $6 a^{2}-11 a b-10 b^{2}$,
(c) $6 a^{2}-11 a b-10 b^{2}-8 a+20 b$.
(4 marks)
4. The marked price of a vase is $\$ 480$. The vase sold at a discount of $25 \%$ on the marked price.
(a) Find the selling price of the vase.
(b) If the profit percentage is $20 \%$, find the cost of the vase.
5. In the figure, if $\angle A D B=25^{\circ}, \angle B D C=40^{\circ}$ and $A B=4 \mathrm{~cm}$, find $B C$ and $\angle A O C$. (4 marks)


## Section A(2) (24 marks)

6. In the figure, $A Q$ is a diameter of the circle $A P O Q$ and $\angle A P O=150^{\circ}$. Find $\angle A Q O$ and $\angle Q A O$.

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Answers written in the margins will not be marked.
7. Consider $f(x)=x^{3}+5 x^{2}-k x-5$, where $k$ is a real constant. When $f(x)$ is divided by $x+2$, the remainder is 9 .
(a) Prove that $x+5$ is a factor of $f(x)$. (4 marks)
(b) Amy claims that all the roots of $f(x)=0$ are distinct. Do you agree? Explain your answer.
(2 marks)

Answers written in the margins will not be marked.
8. The figure shows the graph of $y=-x^{2}+3 x+4$.
(a) Find the coordinates of $A, B$ and $C$.
(b) Find the area of $\triangle A B C$.
(c) Find the coordinates of the vertex of the graph.
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9. The equations of $L_{1}$ and $L_{2}$ are $x-y+2=0$ and $a x+2 y-8=0$ respectively.
(a) If $L_{1}$ and $L_{2}$ are perpendicular to each other, find the value of $a$.
(b) Find the point of intersection of $L_{1}$ and $L_{2}$.
(c) Find the equation of straight line passing through the $y$-intercept of $L_{1}$ and parallel to $L_{2}$.
Section B (28 marks)
10. Solve the equation $1029 \cdot 49^{x+1}=3$.
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11. Solve the equation $\log (2 x+1)+\log (3 x-7)=\log (11 x+1)$.
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12. If $a+6 i=\frac{b i}{3-i}$, find $a$ and $b$.
13. Solve the equation $9^{x}-5 \cdot 3^{x}+4=0$. ( 3 marks)
正
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14. Consider the equation $k x^{2}+2 x-6=0$.
(a) Find the range of values of $k$ if the equation has no real roots.
(2 marks)
(b) Let $\alpha$ and $\beta$ be the roots of the above equation by using the greatest integral value of $k$ in
(a). Form an equation with roots $\alpha-2$ and $\beta-2$.
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Answers written in the margins will not be marked.
15. In the figure, $D O A, F C A$ and $E B A$ are straight lines. $F A$ and $E A$ are the tangents to the circle $B C D$ at $C$ and $B$ respectively.

(a) Find $\angle B O A$.
(b) Show that $\triangle A B D \cong \triangle A C D$.
(c) Hence find $\angle D B E$.
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15 continued

Answers written in the margins will not be marked.
16. The figure shows the linear relation between $\log _{9} y$ and $\log _{3} x$. The slope and the intercept on the vertical axis of the graph are 3 and 5 respectively. Express the relation between $x$ and $y$ in the form $y=A x^{k}$, where $A$ and $k$ are constants.
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## End of Paper

Answers written in the margins will not be marked.

