## 2018-2019 F. 5 2nd TERM EXAM-MATH-CP2



# MATHEMATICS Compulsory Part 

PAPER 2

6th June, 2019
11:00 am - 12:15 pm (1 hour 15 minutes)

## INSTRUCTIONS

1. Read carefully the instructions on the Answer Sheet. After the announcement of the start of the examination, you should insert the information required in the spaces provided.
2. When told to open this book, you should check that all the questions are there. Look for the words 'END OF PAPER' after the last question.
3. All questions carry equal marks.
4. ANSWER ALL QUESTIONS. You should use an HB pencil to mark all your answers on the Answer Sheet, so that wrong marks can be completely erased with a clean rubber. You must mark the answers clearly; otherwise you will lose marks if the answers cannot be captured.
5. You should mark only ONE answer for each question. If you mark more than one answer, you will receive NO MARKS for that question.
6. No marks will be deducted for wrong answers.

There are 30 questions in Section $A$ and 15 questions in Section B.
The diagrams in this paper are not necessarily drawn to scale.
Choose the best answer for each question.

## Section A

1. $\frac{\left(9 k^{-2}\right)^{2}}{3 k^{2}}=$
A. $\frac{6}{k^{2}}$.
B. $\frac{27}{k^{2}}$.
C. $\frac{6}{k^{6}}$.
D. $\frac{27}{k^{6}}$.
2. If $3 x^{4}+5 x^{3}-k x-12$ is divisible by $x+1$, find the value of $k$.
A. -14
B. -4
C. 4
D. 14
3. $0.9274563=$
A. 0.93 (correct to 3 decimal places).
B. 0.9274 (correct to 4 significant figures).
C. 0.92746 (correct to 5 significant figures).
D. 0.92746 (correct to 6 significant figures).
4. If $2 h-k=4 h+3 k=-5$, then $k=$
A. -2 .
B. -1 .
C. 1 .
D. 2 .
5. If $h$ and $k$ are constants such that $m x+(x-3)^{2} \equiv x^{2}+10 x+n$, then
A. $m=10$ and $n=-9$.
B. $m=10$ and $n=9$.
C. $m=16$ and $n=-9$.
D. $m=16$ and $n=9$.
6. If $k$ is a constant such that the quadratic equation $k x^{2}+(3 k+3) x+25=0 \quad$ has equal roots, then $k=$
A. -1 .
B. -5 or 5 .
C. $\frac{1}{9}$ or 9 .
D. $-\frac{1}{9}$ or -9 .
7. The figure shows the graph of $y=a(x+b)^{2}$, where $a$ and $b$ are constants. Which of the following is true?

A. $a>0$ and $b>0$
B. $a>0$ and $b<0$
C. $a<0$ and $b>0$
D. $a<0$ and $b<0$
8. If $a>b>0>k$, which of the following must be true?
I. $\quad \frac{1}{a}>\frac{1}{b}$
II. $\frac{1}{b}>\frac{1}{k}$
III. $a k>b k$
A. I only
B. II only
C. I and III only
D. II and III only
9. Solve $-5-3 x>1$ and $\frac{2 x}{3}-1>3$.
A. $x<-2$
B. $x>6$
C. $-2<x<6$
D. no solution
10. If the base and the height of a right-angled triangle are both increased by $x \%$ so that the area of the triangle is increased by $125 \%$, then $x=$
A. 25 .
B. 50 .
C. 125 .
D. 150 .
11. If $a$ and $b$ are non-zero numbers such that $(4 a+2 b):(5 b-a)=9: 7$, then $a: b=$
A. 17:43.
B. $31: 37$.
C. $37: 31$.
D. $43: 17$.
12. If $z$ varies directly as square root of $x$ and inversely as square of $y$, which of the following must be constant?
A. $\frac{x^{2} z}{y^{2}}$
B. $\frac{y^{2} z}{x^{2}}$
C. $\frac{x z^{2}}{y^{4}}$
D. $\frac{y^{4} z^{2}}{x}$
13. The lengths of two wires are measured as 20 cm and 4 cm respectively, correct to the nearest cm . Find the lower limit of the difference between the actual lengths of two wires.
A. 15 cm
B. 15.5 cm
C. 16 cm
D. 17 cm
14. In the figure, $A E B$ is a straight line.


Which of the following must be true?
I. $a+b=d$
II. $a+c=360^{\circ}$
III. $c+d=b+180^{\circ}$
A. I and II only
B. I and III only
C. II and III only
D. I, II and III
15. In the figure, $A B C D$ and $B E D F$ are parallelograms. $E$ is a point lying on $B C$ such that $B E: E C=2: 3 . A C$ cuts $B F$ and $D E$ at $G$ and $H$ respectively. If the area of $\triangle A B G$ is $135 \mathrm{~cm}^{2}$, then the area of the quadrilateral $D F G H$ is

A. $60 \mathrm{~cm}^{2}$.
B. $81 \mathrm{~cm}^{2}$.
C. $90 \mathrm{~cm}^{2}$.
D. $144 \mathrm{~cm}^{2}$.
16. In the figure, $A D C$ is a straight line. $\angle A B C=\angle A D B=90^{\circ}$. If $A B=k$, then $C D=$
A. $k \cos \theta$.
B. $\frac{k}{\cos \theta}$.
C. $\frac{k \cos \theta}{\sin ^{2} \theta}$.
D. $\frac{k \sin ^{2} \theta}{\cos \theta}$.

17. $\frac{\sin \left(180^{\circ}-\theta\right)}{\cos \theta}-\frac{\cos \theta}{\cos \left(90^{\circ}+\theta\right)}=$
A. 1.
B. $\frac{1}{\sin \theta \cos \theta}$.
C. $\sin \theta \cos \theta$.
D. $1+\tan ^{2} \theta$.
18. In the figure, $A C$ is a diameter of the circle. $A C$ and $B D$ intersect at $E$ such that $B E=D E$. If $\angle C B E=22^{\circ}$, then $\angle A D E=$
A. $46^{\circ}$.
B. $56^{\circ}$.
C. $68^{\circ}$.
D. $78^{\circ}$.

19. In the figure, $3 A B=2 B C=6 C D$. If $\angle A B C=100^{\circ}$, then $\angle A C D=$
A. $60^{\circ}$.
B. $72^{\circ}$.
C. $84^{\circ}$.
D. $96^{\circ}$.

20. In the figure, the bearing of $B$ from $A$ is
A. $030^{\circ}$.
B. $060^{\circ}$.
C. $210^{\circ}$.
D. $240^{\circ}$.

21. If an exterior angle of a regular $n$-sided polygon is $(n+2)^{\circ}$, which of the following is / are true?
I. The value of $n$ is 20 .
II. Each interior angle of the polygon is $160^{\circ}$.
III. The number of folds of rotational symmetry of the polygon is 18 .
A. I only
B. II only
C. I and III only
D. II and III only
22. $A(-12,2)$ and $B(-8,-3)$ are two points in the rectangular coordinate plane. $A$ is rotated clockwise about the origin $O$ through $90^{\circ}$ to $A^{\prime}$. The equation of the straight line passing through $A^{\prime}$ and $B$ is
A. $3 x-2 y+18=0$.
B. $3 x+2 y+30=0$.
C. $2 x-3 y+32=0$.
D. $2 x+3 y+25=0$.
23. The equations of the straight lines $L_{1}$ and $L_{2} \quad$ are $\quad x+2 y=0$ and $\quad 2 x-y=0$ respectively. If $P$ is a moving point in the rectangular coordinate plane such that the perpendicular distance from $P$ to $L_{1}$ is equal to the perpendicular distance from $P$ to $L_{2}$, then the locus of $P$ is a
A. pair of parallel lines.
B. pair of perpendicular lines.
C. straight line.
D. circle.
24. In the figure, the equations of the straight lines $L_{1}$ and $L_{2}$ are $a x+b y+1=0$ and $c x+d y-1=0$ respectively. Which of the following must be true?

I. $\quad a c<0$
II. $\quad b d>0$
III. $a d>b c$
A. I only
B. II only
C. I and III only
D. II and III only
25. The polar coordinates of the points $P, Q$ and $R$ are $\left(3,160^{\circ}\right),\left(4,280^{\circ}\right)$ and $\left(6,340^{\circ}\right)$ respectively. The perpendicular distance from $Q$ to $P R$ is
A. 2 .
B. 3 .
C. $2 \sqrt{3}$.
D. $3 \sqrt{3}$.
26. The equation of the circle $C$ is $-x^{2}-y^{2}+4 x+k y+20=0$. If the radius of $C$ is 5 units and the centre of $C$ lies in quadrant IV, then $k=$
A. -2 .
B. 2 .
C. -2 or 2 .
D. -4 or 4 .
27. In a test, there are two questions. The probability that Karen answers the first question correctly is 0.3 and the probability that Karen answers the second question correctly is 0.4 . The probability that she answers at least one question correctly is
A. 0.88
B. 0.58
C. 0.46
D. 0.42
28. $12 \boldsymbol{\nabla}$ is a 4 -digit number, where $\boldsymbol{\nabla}$ and - are integers from 0 to 9 inclusive. Find the probability that the 4 -digit number is divisible by 5 but not divisible by 10 .
A. $\frac{1}{10}$
B. $\frac{9}{50}$
C. $\frac{1}{5}$
D. $\frac{49}{50}$
29. The box-and-whisker diagram below shows the distribution of the heights (in cm ) of students in a class. If the inter-quartile range of the heights of the students is 24 cm , find $x$.

A. 152
B. 150
C. 148
D. 146
30. Consider the following 10 integers:

$$
\begin{array}{lllll}
2 & 2 & 5 & 5 & 5 \\
x & 6 & 6 & 7 & 7
\end{array}
$$

Let $a, b$ and $c$ be the mean, mode and median of the above integers respectively. Given that the range of the above integers is greater than 5 , which of the following must be true?
I. $\quad a \neq 5$
II. $b=5$
III. $c>5$
A. I and II only
B. I and III only
C. II and III only
D. I, II and III

## Section B

31. $\frac{1}{x^{2}-1}-\frac{1}{x-1}=$
A. $\frac{x}{1-x^{2}}$.
B. $\frac{x-2}{1-x^{2}}$.
C. $-\frac{x}{(x-1)^{2}}$.
D. $\frac{2-x}{(x-1)^{2}}$.
32. The graph in the figure shows the linear relation between $\log _{2} x$ and $\log _{2} y$. Which of the following must be true?
A. $y=3 x^{3}$
B. $y=8 x^{3}$
C. $y=8 x^{4}$
D. $y=x^{3}+8$

33. $11 \times 16^{11}+12 \times 16^{7}+515=$
A. A000B0000201 ${ }_{16}$.
B. $\mathrm{B} 000 \mathrm{C} 0000203_{16}$.
C. A000B000020 ${ }_{16}$.
D. $\mathrm{B} 000 \mathrm{C} 000023_{16}$.
34. Let $k$ be a constant. If the roots of the quadratic equation $x^{2}+k x=2 k$ are $\alpha$ and $\beta$, then $\alpha^{2}+\beta^{2}=$
A. $k^{2}$.
B. $-k^{2}+4 k$.
C. $k^{2}-4 k$.
D. $k^{2}+4 k$.
35. Find the imaginary part of $\frac{2 i^{12}+3 i^{13}+4 i^{14}+5 i^{15}+6 i^{16}}{1-i}$.
A. -3
B. -1
C. 1
D. 3
36. Let $O$ be the origin. $A$ and $B$ are points lying on the positive $x$-axis and the positive $y$-axis respectively such that the equation of $A B$ is $4 x+3 y-12=0$. If a circle is inscribed in $\triangle O A B$ and touches $A B$ at $P$, find the coordinates of $P$.
A. $\left(1, \frac{8}{3}\right)$
B. $\left(\frac{6}{5}, \frac{12}{5}\right)$
C. $\left(\frac{9}{5}, \frac{8}{5}\right)$
D. $\left(2, \frac{4}{3}\right)$
37. Consider the following system of inequalities:

$$
\left\{\begin{array}{c}
y \leq 9 \\
x-y-9 \leq 0 \\
x+y-9 \geq 0
\end{array}\right.
$$

Let $D$ be the region which represents the solution of the above system of inequalities. If $(x, y)$ is a point lying in $D$, then the least value of $x-2 y+43$ is
A. 25 .
B. 43 .
C. 52 .
D. 61 .
38. Which of the following may represent the graph of $y=f(x)$ and the graph of $y=f(-x)+1$ on the same rectangular coordinate system?
A.

B.

C.

D.

39. For $0^{\circ} \leq \theta \leq 360^{\circ}$, how many roots does the equation $3 \cos ^{2} \theta=\cos \theta+2$ have?
A. 2
B. 3
C. 4
D. 5
40. Let $h$ and $k$ be constants. If the figure shows the graph of $y=h \sin k x^{\circ}$, then

A. $h=1, k=\frac{2}{3}$.
B. $h=1, k=\frac{3}{2}$.
C. $h=-1, k=\frac{3}{2}$.
D. $h=-1, k=\frac{2}{3}$.
41. In the figure, $T A$ is the tangent to the circle $A B C D$ at the point $A . C D$ produced and $T A$ produced meet at the point $E$. It is given that $A B=C D \quad, \quad \angle B A T=24^{\circ}$ and $\angle A E D=72^{\circ}$. Find $\angle A B C$.

A. $60^{\circ}$
B. $66^{\circ}$
C. $72^{\circ}$
D. $78^{\circ}$
42. If the variance of the four numbers $a, b, c$ and $d$ are 16 , then the variance of $2(a-2)$, $2(b-2), 2(c-2)$ and $2(d-2)$ is
A. 64 .
B. 32 .
C. 16 .
D. 4 .
43. Let $O$ be the origin. The coordinates of the points $A$ and $B$ are $(0,60)$ and $(96,48)$ respectively. Find the $x$-coordinate of the orthocentre of $\triangle O A B$.
A. 6
B. 32
C. 45
D. 48
44. A queue is formed by 2 boys and 8 girls. If the first two persons in the queue are not boys, find the number of different queues can be formed.
A. 80640
B. 2257920
C. 3548160
D. 3628800
45. In the figure, the area of $\triangle A B C=$

A. $\sqrt{\left(k^{2}+9\right)\left(49-k^{2}\right)} \mathrm{cm}^{2}$.
B. $\sqrt{\left(k^{2}+9\right)\left(49+k^{2}\right)} \mathrm{cm}^{2}$.
C. $\sqrt{\left(k^{2}-9\right)\left(49-k^{2}\right)} \mathrm{cm}^{2}$.
D. $\sqrt{\left(k^{2}-9\right)\left(49+k^{2}\right)} \mathrm{cm}^{2}$.

